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IMPULSIVE LOADING FROM A BARE
EXPLOSIVE CHARGE IN SPACE

by

Joseph Falcovitz
//

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ABSTRACT

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This work is part of a study involving gas dynamics of exhaust plumes from spacecrafts. It was conducted under the cognizance of Distinguished Professor Allen E. Fuhs, who suggested extending our understanding of gasdynamics in space to the treatment of blast effects on spacecrafts. I wish to thank Professor Fuhs for his creative guidance and deeply appreciate his continuous support. The GRP code used for the blast computation is a product of mutual research conducted by Professor M. Ben-Artzi and myself. The fruitful collaboration of Professor Ben-Artzi is gratefully acknowledged.

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NOMENCLATURE (consistent units in m, kg, ms system)

C	Coefficient in ChargeMass-Range-Damage relationship (m kg ^{-1/2})
D _{CJ}	Speed of propagation of detonation wave at CJ point (m ms ⁻¹)
I	Impulse per unit area of target (kg m ⁻¹ ms ⁻¹)
\hat{I}	Dimensionless impulse $\hat{I} = I(R) [4\pi R_0^2/W(2Q_0)^{1/2}]$
h	Beam thickness (m)
L	Length of cantilever beam (m)
m	Lagrange mass coordinate (kg)
M _p	Moment per unit length of plastic hinge (MPa m ²)
N	Number of sub-charges in a cluster configuration
P	Pressure (MPa)
P _s	Surface pressure (MPa)
Q ₀	Explosive energy per unit mass (MJ kg ⁻¹)
R ₀	Radius of spherical charge (m)
R	Range from center of charge (m)
S	Speed of propagation of shock wave (m ms ⁻¹)
t	Time (ms)
U	Flow velocity (m ms ⁻¹)
V	Velocity imparted to target by loading impulse (m ms ⁻¹)
W	Charge mass (kg)
Y	Plastic yield stress (MPa)
Z	Total momentum of an explosive charge (kg m ms ⁻¹)
α	Coefficient for dynamic pressure recovery
γ	Specific-heat ratio
γ_{CJ}	Specific-heat ratio of explosive products at CJ point
θ	Plastic rotation angle of cantilever beam
κ	Impact approximation impulse coefficient (presently $\kappa = 1$)
μ	Beam mass per unit area (kg m ⁻²)
ρ	Fluid density (kg m ⁻³)
ρ_p	Beam density (kg m ⁻³)
ϕ	Mid-area angle of sub-charge spherical cap

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1. INTRODUCTION

The advent of space-based weapon systems in our times has raised the prospects of future "Star Wars" conflicts, rendering the potential use of explosive devices against space targets a present day engineering reality. The warhead of choice in space seems to be of the fragmentation type, for obvious reasons. The effectiveness of fragments is unhampered by the space environment (lack of air may even be helpful). By contrast, bare charges in space are considerably less efficient than in air. One may wonder why this is so since in air, as in space, the same amount of chemical energy is released through the detonation process. The explanation is that the difference is in the much larger mass involved in the air blast, relative to the bare charge mass.

For a more comprehensive explanation, we take a close look at the process by which an explosive-driven air blast wave is generated. The explosive products effectively constitute a rapidly expanding spherical piston (typical initial speed around 6 km/sec), which drives an intense shock wave into the surrounding air. At a typical range of $100R_0$ (and with air density equal to about 1/1000 of charge density), the mass of air entrained by the shock is about 1000 times the charge mass. Thus, the highly concentrated initial explosive energy, has spread over a much larger mass than that of the charge, via the mechanism of wave propagation in compressible media, resulting in an increased momentum. For a comprehensive treatment of blast waves in air the reader is referred to Baker[1].

It is also worthwhile noting that explosive products in space typically attain hypersonic speed prior to impacting at the target. The flow velocity in an air blast is typically subsonic or somewhat supersonic. It is thus expected that the actual gasdynamic interaction between the blast flow and a stationary target, will be fundamentally different in these two cases.

We contend that blast effects in space may still be of practical interest for reasons such as the following :

- (i) Notwithstanding the poor efficiency of a bare charge, its use should not be ruled out altogether. Fragments would contribute to existing - and potentially hazardous - population of space debris, underlining the obvious fact that there is no absolutely safe standoff distance from an isotropic fragmentation warhead. A clean bare charge may thus be a reasonable alternative.
- (ii) Even a fragmentation warhead has some residual blast capacity, which has to be considered either as a factor in enhancing target damage, or as a threat to be reckoned with in determining a safe standoff distance.

The key idea of the present model is a combination of the assumption that target dynamic response is related primarily to total blast impulse, and the physically plausible notion that this impulse is equal to the total momentum of that portion of the expanding explosive products which impacts at the target. The sense in which this simple notion constitutes an approximation to a proper gasdynamic analysis of the interaction between the fluid and the target, is clarified in Ch. 2. In that chapter we also present an illuminating comparison between impulsive blast loading in air and in space.

In order to demonstrate the ChargeMass-Range-Damage relationship implied by our impact blast approximation, we chose a simple target model: A cantilever beam with a rigid-perfectly plastic stress-strain relationship. It represents an extended structural element such as a solar panel or an antenna. We make use of studies conducted by Mentel [2] and by Bodner and Symonds [3], which showed that by and large, the effect of accelerating the beam impulsively was to cause a rotation about a plastic hinge at the point of support. The final angle of rotation is generally proportional to the initial kinetic energy, so that equating damage with that angle, results in damage being proportional to the square of the impulse imparted to the target by the blast loading. A presentation of this dynamic response model, including a sample case, is given in Ch. 3.

Our ChargeMass-Range-Damage relationship may imply some far-reaching conclusions when applied to the analysis of a more general configuration than the single-charge/single-target case. In Ch. 4 we present a simple analysis of a sub-munition configuration of N bare charges, concluding that it seems to have no advantage in efficiency, relative to a single charge of equal mass. Sections 5 and 6 contain conclusions and references, correspondingly.

We conclude the introduction by listing the main assumptions made in the present study:

- (a) Blast loading and target response are uncoupled. This is true since typically the target mass is much larger than the mass of that portion of the explosive products which impacts on it.
- (b) Dynamic target response is independent of specific loading time history. It depends solely on total (time-integrated) impulse.
- (c) The target is a panel extended as a relatively supple cantilever. It is supported by a relatively rigid and massive core structure.
- (d) The charge is a sphere detonated at its center. The expansion is spherically symmetric.
- (e) Target surface is normal to local flow vector.
- (f) Target orbital velocity relative to the center of the charge is negligible, compared with the velocity of the expanding products.

2. IMPACT BLAST LOADING

Consider the expanding explosive products impacting at a target as shown in Fig. 2-1. By regarding the fluid as an ensemble of non-interacting particles moving at velocity $U(R,t)$, and by assuming a no-rebound normal impact at the surface, the pressure time history is given by :

$$P_s(t) = \rho(R,t)[U(R,t)]^2 \quad (2-1)$$

How is this simple impact mechanism related to the actual gasdynamic interaction between the expanding explosive products and the target? When a target is located at a range of at least several charge radii, two features in the free stream of the oncoming fluid are significant : The flow is highly hypersonic (Mach number 20 or higher), and the static pressure is very small, which means that $P + \rho U^2 \approx \rho U^2$. These facts were born out by a numerical computation which we performed for a typical high explosive characterized by the following parameters :

$$\rho_0 = 1800 \text{ (kg m}^{-3}\text{)}$$

$$\gamma_{CJ} = 3$$

$$D_{CJ} = 8 \text{ (m ms}^{-1}\text{)}$$

$$Q_0 = D_{CJ}^2/[2(\gamma_{CJ}^2 - 1)] = 4 \text{ (MJ kg}^{-1}\text{)}$$

Where Q_0 was determined by assuming that the detonation corresponded to the CJ point on the explosive Hugoniot curve, and that the detonation products were an ideal gas with a specific-heat ratio γ_{CJ} . The spherically expanding flow was computed by integrating the Euler equations for isentropic flow via a high-resolution conservative finite-difference scheme [4-6]. The initial conditions were the self-similar flow field of a just-detonated spherical charge given by Taylor [7]. The code GRP with which the computation was performed is described and listed in Appendix A.

Consider the flow at a stationary target, which begins at the moment of arrival of the expanding explosive products (Fig. 2-2). A qualitative description of the ensuing flow pattern is made by observing its evolution in time. Immediately following the initial (normal) impact, the fluid is stopped at the target by a backward-propagating shock wave reflected from the surface. Since the target is of

finite extent, the fluid between the shock and the surface is accelerated laterally, and streamlines that tend to curve around the target are being formed. If the oncoming flow were stationary, the flow field would evolve toward the familiar configuration of a detached bow-shock positioned at a relatively narrow standoff distance from the surface.

Let us find the post-shock pressure in these two limiting phases. In the initial phase, the fluid is stopped at the target by a reflected shock (Fig. 2-3a), and in the pseudo-stationary phase (Fig. 2-3b), the shock is stationary. In either case we find the post-shock pressure to be given by a pressure-recovery expression of the form :

$$P_2 = \alpha \rho U^2 \quad (2-3)$$

Where α is a constant related to the appropriate γ (assuming the expanded explosive products are an ideal gas). The governing equations in the reflected shock case are :

$$\rho(U + S) = \rho_2 S$$

$$\rho(U + S)^2 = P_2 \quad (2-4)$$

$$\rho(\gamma + 1)/(\gamma - 1) = \rho_2 \quad (\text{strong shock})$$

Where the unknowns are ρ_2 , P_2 , S .

The equations for the stationary shock case are :

$$\rho U = \rho_2 U_2$$

$$\rho U^2 = P_2 + \rho_2 U_2^2 \quad (2-5)$$

$$\rho(\gamma + 1)/(\gamma - 1) = \rho_2 \quad (\text{strong shock})$$

Where the unknowns are ρ_2 , U_2 , P_2 . Thus, solving for α in the two cases represented by equations (2-4) and (2-5), we get :

$$\text{Reflected shock} \quad \alpha = [(\gamma + 1)/2]^2 \quad (2-6)$$

$$\text{Stationary shock} \quad \alpha = 2/(\gamma + 1)$$

In either case, since the gas is not dense, the effective range of γ is somewhere between 1.0 and 1.4, so that setting $\alpha = 1$ is an approximation commensurate with the overall crudeness of the present impact blast model. Since the flow in the layer between the shock and the target is low subsonic (at least it is so away from target edges), the post-shock pressure is a reasonable substitute for the surface pressure. Also, $\alpha = 1$ is an appropriate approximation where the flow is so rarefied that it is collisionless. In this limit, $\alpha = 1$ corresponds to full thermal accommodation of re-emitted molecules from a presumably cold surface.

The foregoing analysis constitutes a justification of the impact approximation to the surface pressure (2-1). Now we turn to the task of evaluating the impulse which is defined as the time-integrated surface pressure. Using the impact approximation (2-1), the impulse is given by :

$$I(R) = \int_0^\infty P_s(t)dt = \int_0^\infty \rho(R,t)[U(R,t)]^2dt \quad (2-7)$$

Let us introduce a Lagrange mass coordinate m which enables a transformation from the Euler system (R,t) to the Lagrange system (m,t) . The differential relation associated with this transformation at constant R is :

$$dm = 4\pi R^2 \rho(R,t) U(R,t) dt \quad (2-8)$$

Since it is assumed that the fluid is not accelerated at any (R,t) in the range of interest for blast loading, the velocity $U(R,t)$ can be regarded as function *solely of the mass coordinate*, so that $U(R,t) = U(m)$. Using (2-8) we are then able to cast the impact blast expression (2-7) in the following simple and physically appealing form :

$$I(R) = Z/4\pi R^2$$

$$Z = \int_0^W U(m) dm \quad (2-9)$$

The upper limit W in (2-9), which is consistent with the upper limit ∞ in (2-7), implies that the total impulse is somewhat overestimated, since it contains contributions from the innermost layers of the explosive products that will arrive at the target as $t \rightarrow \infty$.

The total momentum Z is thus a constant which can be evaluated for any specific explosive charge by numerical integration. We performed this computation with the code GRP described in Appendix A. In doing so for the typical explosive (2-2), we found out that the impulse (2-9) was a reasonable approximation at ranges as low as $R = 3R_0$. Furthermore, it was found that Z could be approximated by the maximum attainable momentum for the given charge mass and energy $W(2Q_0)^{1/2}$, to within about 6%. Apparently, the total momentum is not overly sensitive to the exact velocity distribution function $U(m)$, so that assuming a value of Z appropriate to the uniform distribution $U(m) = (2Q_0)^{1/2}$ is a reasonable approximation. Thus we finally arrive at the following closed-form approximation for the blast impulse :

$$I(R) = \kappa W(2Q_0)^{1/2} / 4\pi R^2 \quad (2-10)$$

$$\kappa = 1$$

Where the coefficient κ is retained in order to suggest that its value be determined more accurately from detailed experimental or computational data, in the event that such data become available. At present our best estimate is $\kappa = 1$.

There is one comparison, however, which can readily be made with available data. We refer to impulsive blast loading in air, such as given by Baker (Ref. 1, Fig. 6.3 in the supplement). The comparison is conveniently made with a non-dimensional form of (2-10), which is rewritten as :

$$\hat{I} = I(R) [4\pi R_0^2 / W(2Q_0)^{1/2}] = (R/R_0)^2 \quad (2-11)$$

The air blast data has to be converted to the same normalization scheme as in Eq. (2-11), before the comparison can be made. Considering the definition of \hat{I} in (2-11) above, and the definition of scaled range and air blast impulse (Table 6.2 of Ref. 1), this conversion is done by multiplying the scaled air impulse and range by the following coefficients (sea-level air is assumed) :

$$\text{Impulse Multiplier} \quad \beta = 3(2\gamma)^{-1/2} (4\pi/3)^{1/3} (P_a/\rho_a Q_0)^{1/6} (\rho_a/\rho_0)^{1/2} = .01204$$

$$\text{Range Multiplier} \quad \delta = (4\pi/3)^{1/3} (\rho_0 Q_0 / P_a)^{1/3} = 67.06 \quad (2-12)$$

$$\rho_a = 1.3 \text{ (kg m}^{-3}\text{)} \quad P_a = 0.1 \text{ (MPa)} \quad \gamma = 1.4$$

The air blast conversion was done by a small code which is given in Appendix B. The air and space blast impulses are shown in Fig. 2-4. We note that at ranges larger than about 10 charge radii, the air blast impulse is higher than the space impulse, and the gap widens as the range increases. This observation is consistent with the qualitative explanation given in the introduction, which attributed this effect to the increase in the entrained air mass at higher range. At ranges lower than 10 charge radii, the air mass is relatively insignificant, so that one may expect the blast impulses in air and in space to be comparable. Indeed, the inverse-square variation of impulse with range is apparent for the air blast at low range. In absolute values, however, the low-range space impulse is higher by a factor of about 1.7. This might be interpreted as indicating that choosing $\kappa = 1/1.7$ would be the appropriate "calibration". However, we do not propose to do so, since we are not able to trace the various factors affecting the low-range impulse as given by Baker [1]; they may somehow depend on the presence of air, as well as on other parameters such as target size and equation of state of the explosion products.

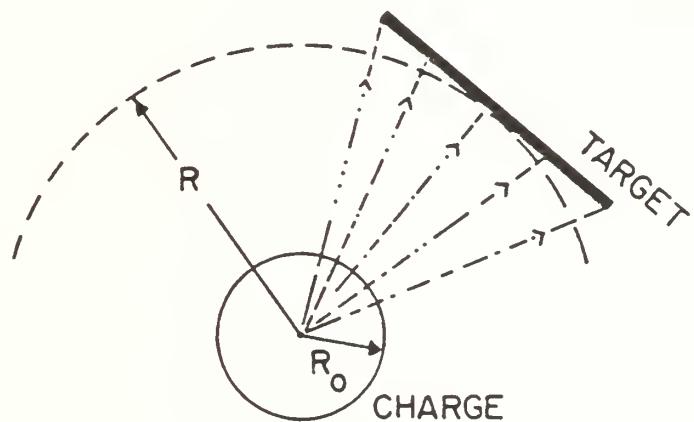


Figure 2-1. Impact Blast Loading

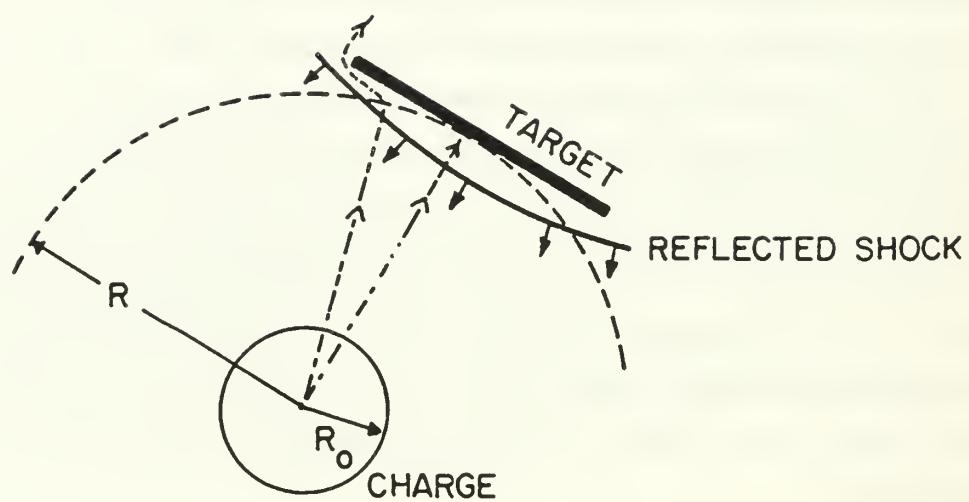
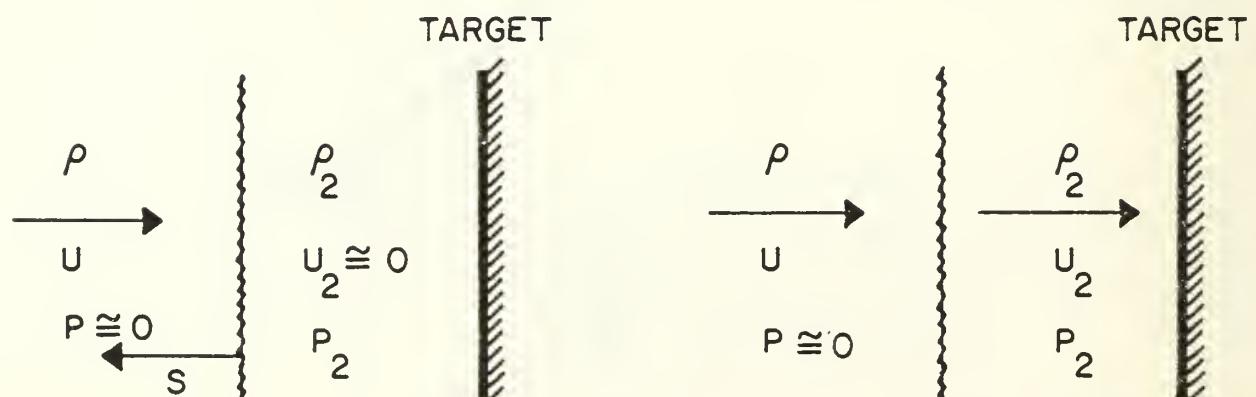


Figure 2-2. Shock Reflection at Impact Phase



(a) Initially Reflected Shock (Impact)

(b) Stationary Shock

Figure 2-3. Limiting Cases of Shock Reflection

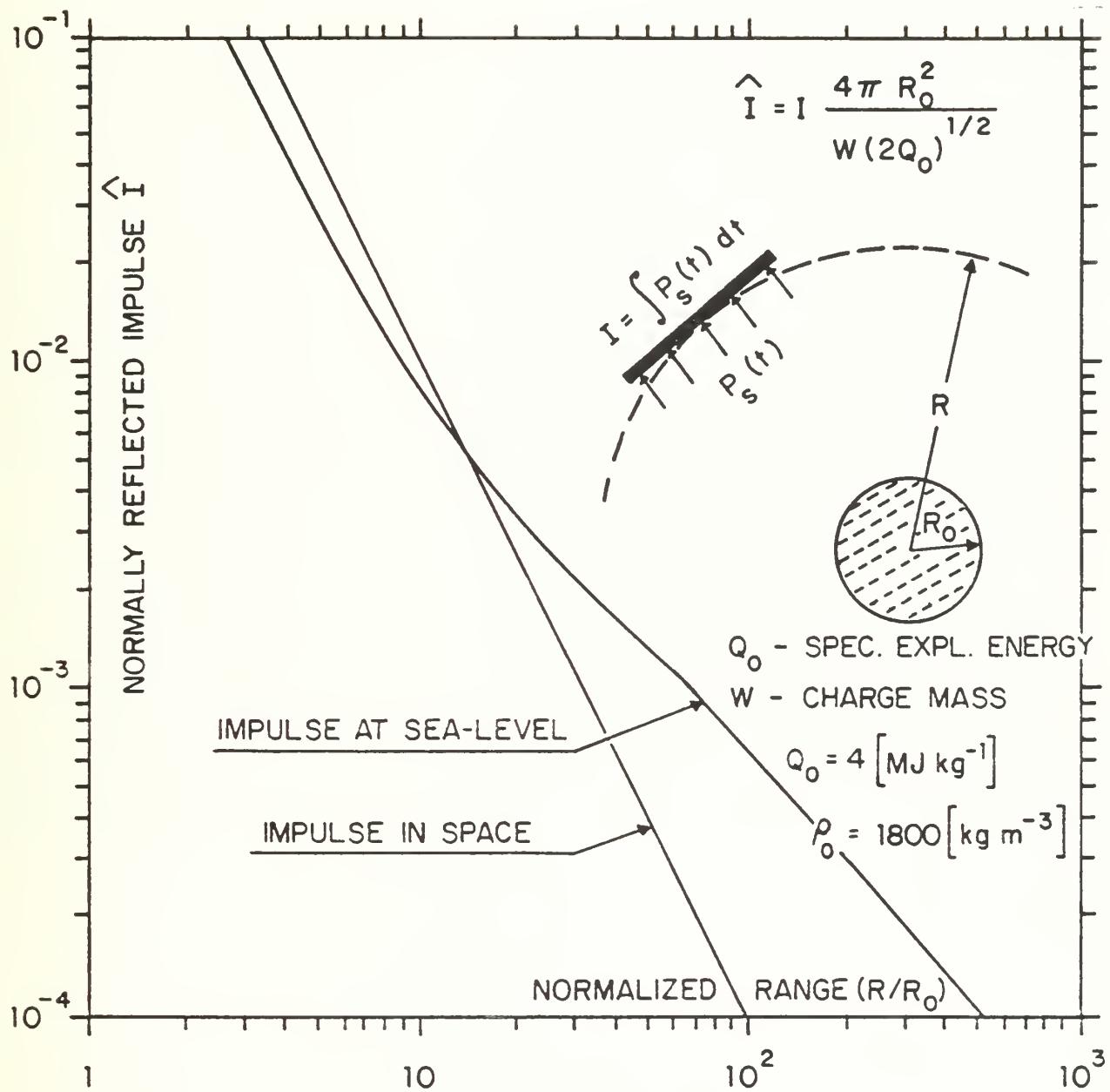


Figure 2-4. Impulse of Normally Reflected Blast Wave at Sea-Level and in Space

3. TARGET DYNAMIC RESPONSE

For the sake of constructing representative Charge-Mass-Range-Damage relations from our impact approximation to the blast impulse (2-10), we suggest a simple idealized structure as target model. It is a cantilever beam made of a metal characterized by a rigid-perfectly plastic stress-strain relation.

This model is supposed to represent an extended spacecraft component such as a solar panel or an antenna. The core structure is assumed to be much more massive and rigid than the extended structural element, so that the cantilever can be idealized as being rigidly supported. The sole dynamic and structural parameters are hence those of the cantilever.

For this purpose we make use of an experimental and theoretical investigation of uniform cantilever beams subjected to impulsive loading that was conducted by Mentel [2]. Aluminum alloy beams were held in a massive support that was gliding along a rail at speed V , until it was abruptly stopped by a very massive anvil. After the system came to rest, the beams were observed to have rotated through an angle θ about the point of support, with little deformation elsewhere (Fig. 3-1).

The theoretical model suggested by Mentel [2] for predicting $\theta(V)$, can be described as comprising two stages. Immediately following the impact, the beam commences rotating rigidly about the support point, with an angular momentum equal to the pre-collision moment of momentum about that point. This application of the principle of conservation of moment of momentum entails an abrupt re-distribution of velocity in the beam, with velocity being proportional to distance from support, and the tip moving at $1.5V$. The angle θ is subsequently determined from the requirement that the rotational kinetic energy be dissipated as plastic hinge work $M_p\theta$. The resulting $\theta(V)$ expression is :

$$\theta = (3/8)\mu LV^2/M_p \quad (3-1)$$

We now make one more step in formulating the model, in that we postulate that *the angle θ is a measure of damage*. Using the following expressions for M_p , μ and V :

$$M_p = (1/4)Yh^2$$

$$\mu = \rho_p h \quad (3-2)$$

$$V = I(R)/\mu$$

We get from (2-10) and (3-1) the following ChargeMass-Range-Damage (W-R-θ) relationship :

$$R = CW^{1/2} \quad (3-3)$$

$$C = [(3/16\pi^2\theta) (LQ_0/\rho_p Yh^3)]^{1/4}$$

We note that the effective range for a specified target and "damage level" θ , is proportional to the square root of the charge mass W .

Using the data for the typical explosive (2-2), and the following data for a specific aluminum beam, we get for this sample case :

$$h = 0.002 \text{ (m)}$$

$$L = 1.0 \text{ (m)}$$

$$\rho_p = 2700 \text{ (kg m}^{-3}\text{)} \quad (3-4)$$

$$Y = 300 \text{ (MPa)}$$

$$C = 1.85 \theta^{-1/4} \text{ (m kg}^{-1/2}\text{)}$$

The ChargeMass-Range-Damage relationship corresponding to this sample case is depicted in Fig. 3-2.

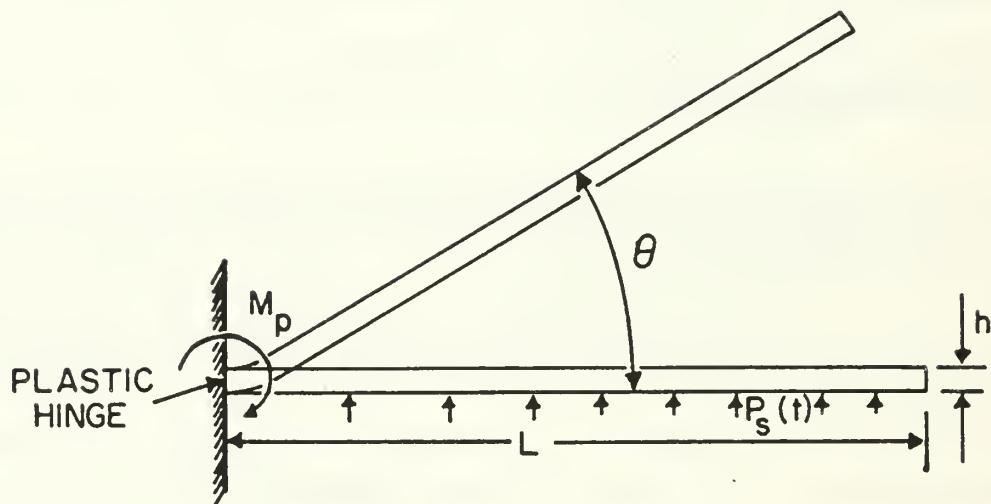


Figure 3-1. Cantilever Beam with Plastic Hinge

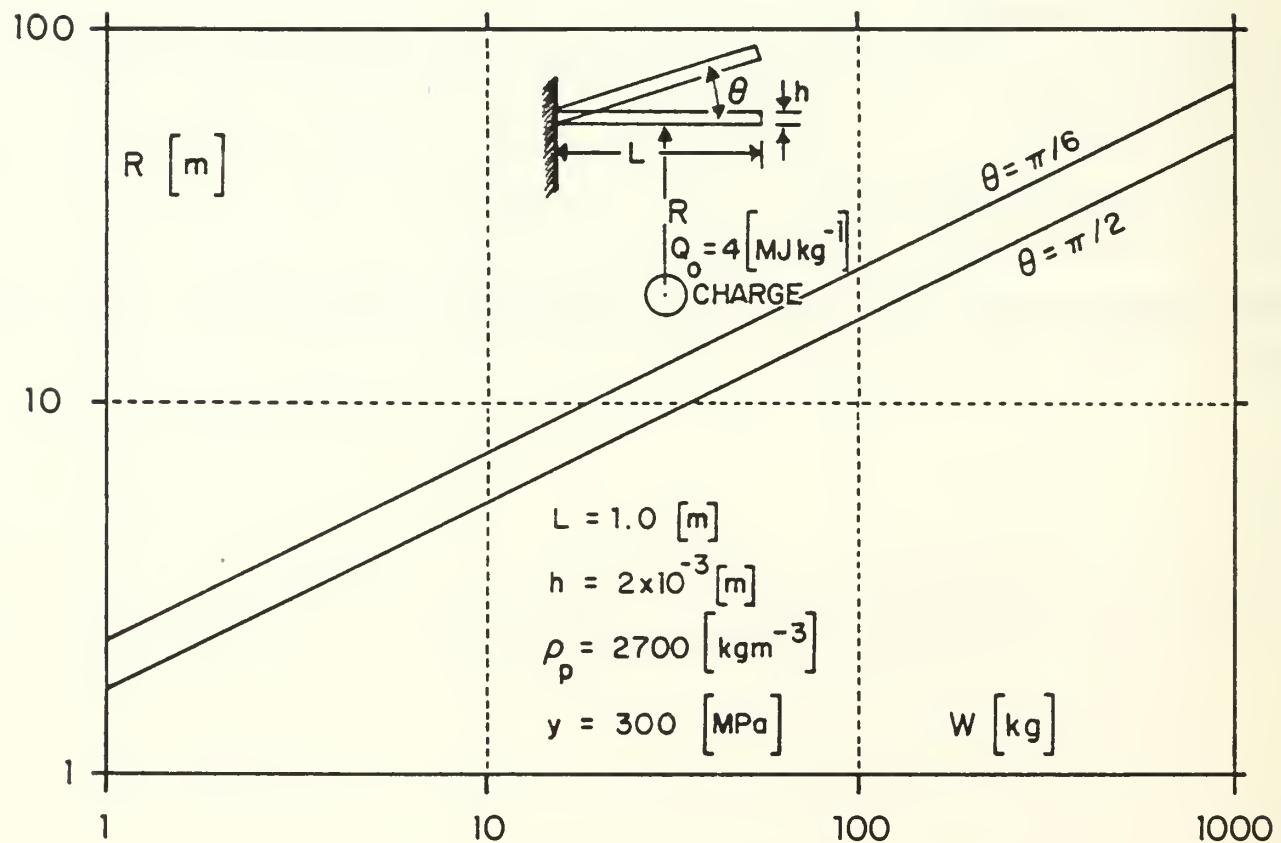


Figure 3-2. ChargeMass - Range - Damage Curves for Cantilever Beam

4. CLUSTER CONFIGURATION

In a cluster configuration, the gain in damage is presumably a result of a favorable design tradeoff between reduced charge mass and reduced range. Can such a gain be achieved for a space system, assuming the ChargeMass-Range-Damage law (3-3) to hold? It can be shown that by adopting some simple strategy of sub-munition dispersion and initiation, equation (3-3) implies no gain in target damage.

Let us assume for the sake of a reasonably simple analysis, that dispersion and initiation of sub-charges would take place according to the following scheme :

- (a) The N sub-charges appear to fan out from a common virtual center, moving at equal speeds. At subsequent times, their centers are uniformly distributed over an expanding spherical envelop.
- (b) The target moves at a constant velocity relative to the virtual center. Its point of closest approach to that center is at range R .
- (c) The timing for dispersion is chosen so that the target intersects (tangentially) with the spherical envelop at the point of closest approach (Fig. 4-1). This is also the point at which the blast from a single-charge configuration detonated at the virtual center, would have impacted at the target.
- (d) All sub-munitions are detonated at this "moment of closest approach".
- (e) It is assumed that each spherical cap of area $4\pi R^2/N$ will contain one, and only one, sub-charge. The probability of the charge location on that cap is assumed to be uniformly distributed. The expected location on the cap is hence that latitude line ϕ which divides the cap into two parts of equal area (Fig. 4-2).
- (f) It is assumed that the target is subjected to the blast of a single sub-charge, which is located on the mid-area latitude ϕ of the spherical cap that surrounds the target (Fig. 4-2).

Since the area of the spherical cap subtended by ϕ is $4\pi R^2/(2N)$, the angle ϕ is given by :

$$\sin(\phi/2) = (2N)^{-1/2} \quad (4-1)$$

We seek a comparison between the deflection θ for a single charge (W, R) , and the deflection θ_N in the sub-munition case ($W_N = W/N$, $R_N = 2R\sin(\phi/2)$). From the ChargeMass-Range-Damage law (3-3), using also Eq. (4-1), we get :

$$(\theta_N/\theta) = (W_N/W)^2 (R/R_N)^4 = 1/4 \quad (4-2)$$

Consequently, there is no potential gain in a tradeoff between charge mass and range, for a cluster configuration with the aforementioned dispersion scheme. The factor $1/4$, along with the mass overhead inherent in constructing a multi-charge configuration, indicate that in causing blast damage, a single charge is more effective than an equal-mass isotropically dispersed cluster.

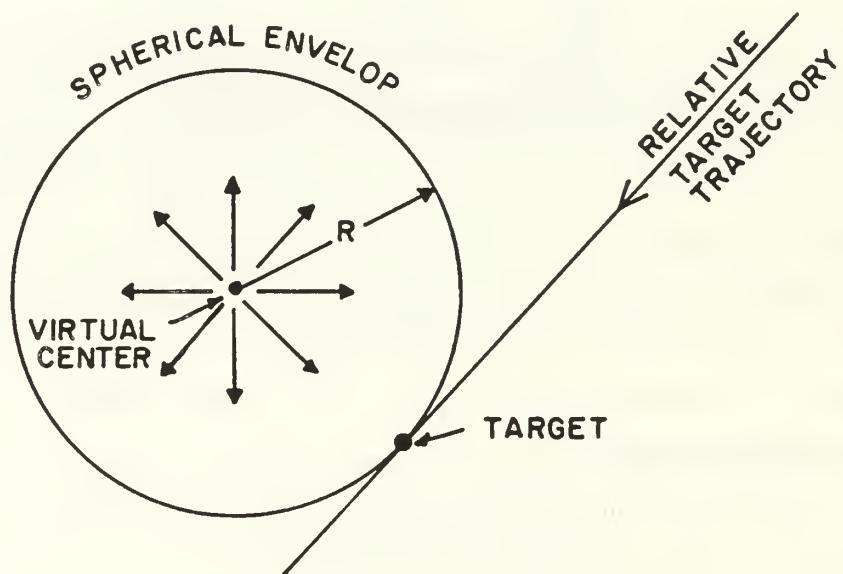


Figure 4-1. Target Intercept at Closest Approach

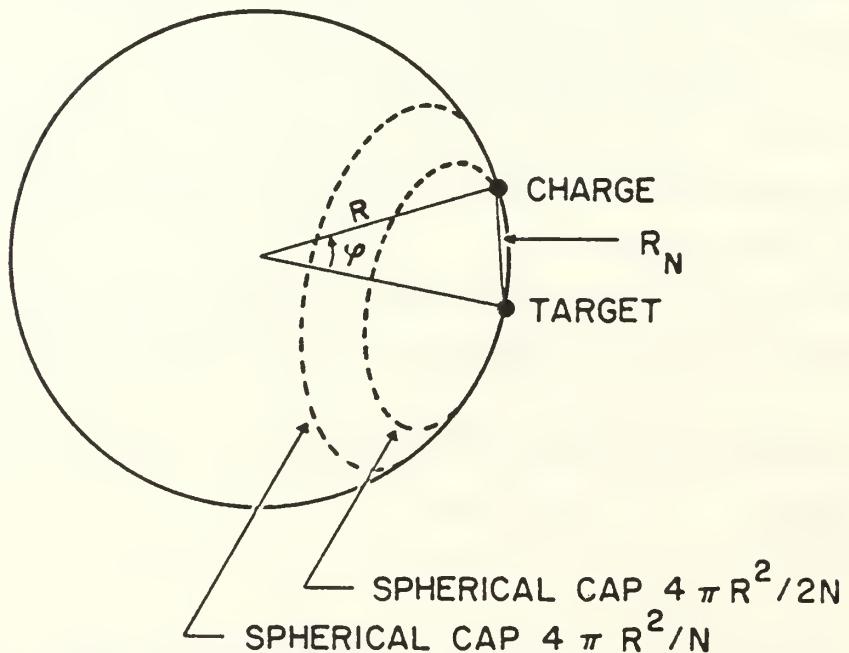


Figure 4-2. Spherical Cap Surrounding the Target

5. DISCUSSION AND CONCLUSIONS

Our analysis pertains to a bare explosive charge initiated at a point of closest approach to the target. We have shown that the loading impulse on a planform target is given by the impact approximation (2-7), which states that the impulse is proportional to the charge mass and inversely proportional to the range squared. The impulse in space has been compared with impulse in air at sea-level. It was found that the two are quite comparable at close range (10 charge radii or less), exhibiting identical variation with range. At far ranges, the impulse in air is the higher one. This is consistent with the notion that spreading the explosive energy over larger air mass results in larger momentum (and hence reflected impulse). We then proceeded to develop the ChargeMass-Range-Damage law (3-3) for an impulse-responsive target, which states that blast damage is proportional to the square of the charge mass and inversely proportional to the fourth power of the range. These results were obtained by introducing extensive simplifications in the analysis of gasdynamic interaction, and in the analysis of dynamic target response. We have further shown that this damage law also implies that no gain can be achieved by an idealized cluster configuration of bare sub-charges, relative to a single charge of equal total mass.

It is worthwhile noting that all assumptions introduced in the course of formulating the impact blast approximation and the structural dynamic response to impulsive loading, imply that target damage is overestimated. The only exception is the approximation in setting $\alpha = 1$, which can be readily rectified by assigning to α the reflected shock value given in (2-6). Furthermore, we assumed that the pressure at the midpoint of the target, is the pressure everywhere on the target. Due to flow around the edges, the average pressure is lower than the midpoint pressure. Also, targets are not everywhere normal to the flow (and charge/target attitude is not a design parameter). Oblique impact obviously entails reduced target loading. In the area of structural dynamic response, a time-distributed loading function generally delivers less kinetic energy to the structure than an impulsive loading of equal total impulse, resulting in reduced deformation (damage). Thus, while the present model may be regarded as an over estimate when applied to a sure-fail analysis, it is particularly suitable in determining a sure-safe range.

6. REFERENCES

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APPENDIX A. The GRP Code

The purpose of this Appendix is to provide a concise description of the GRP code, and a listing of its CHARGE version. It is intended for users that have had prior experience in implementing schemes for solving the Euler equation of compressible flow. The theoretical background of GRP schemes constitutes the principles on which the code is founded. Some familiarity (at least) with this background, as given in References 4, 5 and 6 is indispensable to any implementation of GRP schemes. Reference 4 is recommended as an introduction. The planar GRP scheme is fully described in Reference 5, and the duct-flow GRP scheme on which the present CHARGE version is based is given in Reference 6. (In CHARGE version the flow is spherical and the "duct" area is set to $X(I)^{**2}$, but the code can handle any area variation - see subroutines CROSS and RATIO below).

In GRP schemes, second-order accuracy is achieved by considering a piecewise linear interpolation of the flow in each cell (Fig. A-1), from which second-order accurate fluxes at each cell interface are evaluated through an analysis of a local Generalized Riemann Problem (GRP). Briefly stated, the GRP goes one step further than the Riemann Problem (RP), in that it seeks (analytically) the first time-derivative of the flow that evolves as the "diaphragm" is removed from the cell interface, at the origin of the centered (X,T) wave paths of the RP solution. The major computational subroutines are CYCEUL where the integration of conservation laws is performed, RIEMAN where the local Riemann Problems are solved by Newton-Raphson iterations, MAGA where the closed-form expressions derived from the GRP analysis [6] are used to compute flow time-derivatives along the contact surface, FLUXE where all the previously computed information is used to extrapolate the fluxes to mid-time-step ($T + DT/2$) which constitutes a second-order accurate flux.

The plan of this Appendix is as follows. Array variables, including those which carry conserved variables (mass, momentum and energy), are described in section A.1. This is followed by descriptions of general parameters (A.2), labeled COMMON variables (A.3) and all subroutines (A.4). We conclude by giving the CHARGE version listing (A.5), which should be consulted whenever a reading of this code description is attempted.

NOTE : The present CHARGE version was implemented in a GRP code version that had been converted to treat detonation waves as chemically reactive compressible flow. However, the detonation scheme is effectively neutralized by setting QDET=0 (in NETUNM). All variables pertaining to detonation, such as arrays Z(I), DZ(I), FIMZ(I), ZMDOT(I) and labeled COMMON variables containing Z in their names, should be ignored.

A.1 Array Variables

The code GRP is organized so that all major subroutines are called with standard list of array variables which represent the integration scheme (i.e. the conservation laws), local Riemann Problem solutions and second-order accurate fluxes. Virtually all array variables are initially defined in BEGIN (initial conditions), and are subsequently updated at each time step in CYCEUL. The following list explains the meaning of these variables. Some terms used in the list are defined below.

X(I)	grid point coordinate.
U(I)	velocity in cell I.
P(I)	pressure in cell I (computed from equation of state).
RO(I)	density in cell I. This variable is time-integrated according to the law of conservation of mass. (Computed in CYCEUL).
E(I)	total energy per unit volume (including kinetic energy) in cell I. This variable is time-integrated according to the law of conservation of (total) energy. (Computed in CYCEUL).
DU(I)	velocity difference in cell I.
DP(I)	pressure difference in cell I.
DRO(I)	density difference in cell I.
DG(I)	Lagrange sound velocity difference in cell I.
DXSI(I)	the Lagrange coordinate increment defined as $RO(I) * (X(I+1) - X(I))$, for cell I.
MIN(I)	inactive in present version.
US(I)	velocity at the contact surface obtained after the resolution of the local discontinuity at $X(I)$ (Riemann Problem solution). It is denoted as U^* in References 4-6.
PS(I)	pressure at the contact surface obtained after the resolution of the local discontinuity at $X(I)$ (Riemann Problem solution). It is denoted as P^* in References 4-6.
UIDOT(I)	time derivative of US(I) along the contact surface. (This derivative is the result of the GRP analysis. It is computed in MAGA. See Ref. 5 and 6).
PIDOT(I)	time derivative of PS(I) along the contact surface. (This derivative is the result of the GRP analysis. It is computed in MAGA. See Ref. 5 and 6).
FIMZ(I)	inactive in present version.
ZMDOT(I)	inactive in present version.

TENA(I)	momentum per unit volume $RO(I)*U(I)$ in cell I. This variable is time-integrated according to the law of conservation of momentum. (Computed in CYCEUL).
FIRO(I)	mass flux at point $X(I)$ (second-order accurate).
FIM(I)	momentum flux at point $X(I)$ (second-order accurate).
FIE(I)	energy flux at point $X(I)$ (second-order accurate).
GIP(I)	the pressure term in the momentum flux. It corresponds to $G(U)$ in References 4 and 6.
VOL(I)	volume of cell I.
Z(I)	inactive in present version.
DZ(I)	inactive in present version.

Glossary of terms used in the array variables list :

Cell I - the cell between grid points $X(I)$ and $X(I+1)$. All cell variables are averages per that interval.

Difference in cell I - the difference between values of variable at cell boundaries $X(I+1)$ and $X(I)$. Those values are obtained from "monotonized" piecewise linear distribution of each variable in each cell. (Fig. A-1).

Second-order accurate flux - the flux time-derivative at point $X(I)$ is computed from the time-derivatives of pressure and velocity along contact surface $PIDOT(I)$ and $UIDOT(I)$ (in FLUXE). Then the the flux is extrapolated to the centered time point ($T + DT/2$), using those derivatives. This centered value is the second-order flux for integrating the conservation laws between T and $T + DT$.

A.2 Major Parameters

A list of major parameters indicating their meaning and the routine in which they are defined, is given below. Those parameters defined in NETUNM are the run input. There is no reading of an input file in this version of GRP code (and the only output is the printed output).

L	number of grid points + 1 (main program)
LL	L - 1 (MAIN PROGRAM)
T	time (MAIN0)
DT	time step (MAIN0)
TMAX	maximum time (when T.GE.TMAX the run is terminated) (NETUNM)
TMUD	time for which next printing will take place (NETUNM)
DTMUD	printing time step (NETUNM)
NCYC	serial number of time step (integration cycles) (MAIN0)
COLELA	switch to evaluate cell differences by Colella's method when COLELA.NE.0 (NETUNM)
KEYMON	key for monotonization scheme (just one is presently provided when COLELA.EQ.0) (NETUNM)
NCYCPR	frequency of line printing at each cycle (time step) (NETUNM)
STAB	CFL stability coefficient. Must be smaller than 1. (NETUNM)
DTBA	next time step computed from stability criterion (CYCEUL)
DTKOD	former time step (MAIN0)
KDT	index of cell where DTBA was determined (CYCEUL)

A.3 Labeled COMMON variables

Labeled COMMONs are used primarily to transmit data to and from routines that perform the major computational steps of the GRP scheme, i.e, RIEMAN, MAGA and FLUXE; these routines are called from CYCEUL. When the value of any of those variables is needed for later use, whether for updating conservation variables (RO, TENA, E), or for printing, it is stored in the appropriate array. All labeled COMMON variables are grouped under labels that indicate their role, and their names are also mnemonic. Generally, suffix L means Left and suffix R means Right. It may indicate sides either with respect to a cell interface X(I), or with respect to the contact surface which separates the Right- and Left- propagating waves in a solution to the local Riemann Problem. We indicate by INPUT variables that are computed prior to calling the subroutine, and by OUTPUT variables whose value was computed within the subroutine and constitutes the result of calling that subroutine.

COMMON /STEP0/ Parameters related to the local Riemann Problem. This is the first step in the GRP scheme.

UL, PL, ROL, CL, GL, SL - velocity, pressure, density, sound speed, Lagrange sound speed and entropy, attributed to Left side of cell interface at point X(I). (INPUT)

USTAR, PSTAR - velocity and pressure at the contact surface obtained when the local discontinuity is resolved (i.e., the solution to the local Riemann Problem). The omission of L or R suffix indicates that P and U are continuous across the contact surface. (OUTPUT)

RSTARL, CSTARL, GSTARL - density, sound speed and Lagrange sound speed on the Left side of the contact surface. (OUTPUT)

WL - Lagrange velocity of propagation of the Left-moving shock, relative to the fluid. (OUTPUT)

UW(6) - velocity of propagation of each wave front (Fig. A-3), relative to the inertial system (X). (OUTPUT)

HELEM1 - logical variable. If HELEM1.EQ..TRUE. the Left-propagating wave is a shock. Otherwise it is a (centered) rarefaction wave. (OUTPUT)

NFLUX - integer variable. It denotes the region in the Riemann solution wave structure, which contains the point X(I) for all time. Refer to Fig. A-3 for illustration. (OUTPUT)

LAMDAL, RATEL, TEMPL, TEMPSL, ZL, ZSTARL - inactive.

COMMON /STEP1/ Parameters related to the time-derivative evaluation of the GRP scheme, performed in MAGA. The time-derivatives of P and U along the contact surface are the main result of MAGA.

DUIDT, DPIDT - time-derivatives of velocity and pressure along contact surface. (OUTPUT)

ASTARL - The directional derivative of U along the fan characteristic at the trailing characteristic of the Left rarefaction wave. It is not evaluated when the Left wave is a shock. (See References 4-6) (OUTPUT)

DGIDTL, DRIDTL - time-derivatives of Lagrange sound speed and density along the left side of the contact surface. (OUTPUT)

DSDAL - Lagrange spatial derivative of entropy on the left side of contact surface, prior to removal of the partition at X(I).

SH, RAT - the cross-section area and the x-derivative of $\ln(SH)$. They are user-defined in CROSS and RATIO respectively.

DSDASL - entropy derivative used in the special "sonic" case (i.e, when NFLUX=2 or NFLUX=5). See References 5,6 for details. (OUTPUT)

LAMDSL, DZDAL, BETACL, DZDASL - inactive.

COMMON /GRADS/ Used to transmit flow gradients (that exist in fluid prior to removal of the partition at X(I)) to MAGA.

DUDXIL, DPDXIL, DGDXIL, DRDXIL, DSDXIL - gradients of U, P, G, RO, S (with respect to Lagrange coordinate). They are computed in CYCEUL for transmission to MAGA. (INPUT)

DZDXIL - inactive.

COMMON /FI/ Used to return values of updated flux and cell-interface variables from FLUXE.

FIH1, FIH2, FIH3 - second-order flux of mass, momentum flow (just $RO*U^{**2}$) and energy. They are extrapolated to Half the time step $T + DT/2$. (OUTPUT)

GIH - the value of P at $T + DT/2$

UXN, PNX, GXN, ROXN - values of U, P, G, RO extrapolated to New time T+DT, at cell-interface. They are used in CYCEUL to get tentative (pre-monotonized) new cell differences. (OUTPUT)

ZXN, FIH4, ZMDOTL, ZMDOTR - inactive.

A.4 Description of Subroutines

MAIN PROGRAM

The task of this program is to allocate array space for the NMAT arrays required by the present version of GRP code. The length of each array is L. The allocation is done by calling MAIN0. This standard calling sequence is maintained hereafter, thus facilitating modifications.

MAIN0

This subroutine functions as an overall organization routine. It can be read as a kind of flow-chart of the entire computation. First, run set-up is done by calling once to NETUNM (data) and BEGIN (initial conditions). Then a loop over time steps is begun. In each cycle the integration by one time step is performed by calling CYCEUL, and subsequently boundary conditions are implemented by calling SAFAE. Whenever T.EQ.TMUD, results are printed by calling PRINT and TMUD is updated by adding DTMUD.

NETUNM

Here data are set for a particular run. User is invited to modify this routine. There is no input file. This routine is called just once from MAIN0. Note that the detonation data section is skipped when QDET.EQ.0.

BEGIN

Initial conditions are set-up in this routine. The configuration of some nominal case is given in present version. (In CHARGE version it is the detonated spherical charge, using the Taylor self similar solution as initial conditions). User is called to modify this routine so as to generate any other desired initial configuration.

TAYLOR

The purpose of this routine, along with ancillary routines INIDAT, RUNGE and DERIV, is to compute the self-similar Taylor solution [7] of a detonated spherical charge, and implement it as initial conditions for the GRP computation of the ensuing expansion. TAYLOR is called once by BEGIN.

The core of the solution is the numerical (Runge-Kutta) integration of two coupled ordinary differential equations. The integration variable is PSI. (The flow velocity normalized by DCJ is given

by $U = \text{EXP}(-\text{PSI})$). The two dependent variables are X - the normalized radial coordinate ($X = 1$ at the sphere boundary), and C - the normalized speed of sound. The integration is carried out by calling RUNGE, which in turn calls DERIV for the evaluation of derivatives. Data for the TAYLOR computation is set up by calling (just once) INIDAT.

The initial conditions needed in BEGIN are values of mass, momentum and (total) energy per cell. These are most accurately computed by spatially integrating the Taylor solution, resulting in lumped mass, momentum and energy per cell, which are then divided by the cell volume. This refinement is significant since gradients are high near the charge boundary ($X = 1$). A total mass and energy check for the entire sphere is performed and printed.

INIDAT, RUNGE, DERIV

Subroutines used only in conjunction with the Taylor initial conditions setup. See TAYLOR above.

RATIO, CROSS

User-defined routines. If $A(X)$ is the duct cross-section area, then $CROSS(X) = A(X)$ and $RATIO(X) = D[\ln(A(X))]/DX$.

CYCEUL

This is the central computation routine. All major stages of the GRP scheme are performed by calling specific subroutines from CYCEUL. Then RO(I), TENA(I) and E(I) are updated to new time $T + DT$ by solving the appropriate conservation laws in CYCEUL.

The first loop (DO 1) performs a set of preparatory steps as follows :

- (a) CALL RIEMAN - Solving the local Riemann Problem at each $X(I)$.
- (b) CALL MAGA - Solving the local Generalized Riemann Problem at each $X(I)$.
- (c) CALL FLUXE - Computing second-order fluxes at $X(I)$.
- (d) Evaluation of cell-interface finite differences $DU(I)$, $DP(I)$, $DRO(I)$ in each cell. These will be used at the future time step (after monotonization) for piecewise-linear interpolation of the flow in each cell. (See definition of $DUDXIL$, $DPDXIL$, ..., just preceding the call to MAGA in this loop).

Note that in present CHARGE version additional computation of PRESS, PULSE1, ..., PULSE4 has been added. It is just informative and does not interfere in any way with the execution of the

GRP scheme. The purpose of this computation is to monitor the numerical solution and to observe the accuracy within which the asymptotic value of the momentum integral Z (Eq. 2-9 above) is approached.

In the second loop (DO 2), the integration of the three conservation laws is performed, using second-order fluxes that had been computed in loop 1. Flow variables such as $P(I)$ and $U(I)$ are computed in this loop from the conserved variables. The cycle computation is concluded by calling BDOK1 for monotonization of $DU(I)$, $DP(I)$ and $DRO(I)$.

SAFAE

In this routine user-defined boundary conditions are implemented. Present version (CHARGE) contains rigid wall at the center of the sphere $X(2)=0$, and an "open boundary" at the outer computational zone limit $X(L)$. The rigid wall condition is achieved by setting up a virtual antisymmetric cell next to the boundary cell, so that the solution to the local Riemann Problem will result in a non-moving contact surface ($USTAR=0$). The open boundary is an approximation to an ideally non-reflecting boundary. Here the virtual cell is $I=L$, and the flow in it is defined as a "continuation" of the flow in the adjacent last cell $I=LL$.

BDOK1

Here the tentative cell-interface differences $DV(I)$ are monotonized according to neighboring average cell values $V(I-1)$, $V(I)$ and $V(I+1)$. The basic idea is that the cell-interface slope $DV(I)$ should have the same sign as the average slope $V(I+1)-V(I-1)$. When $V(I)$ is a local extremum $DV(I)$ is set to zero. Also, the absolute value of $DV(I)$ is constrained so that the jump from a cell-interface value to the adjacent average value $V(I)$, will never be of opposite sign to $DV(I)$.

DCOLE

When COLELA option is used (not in present CHARGE version), the pre-monotonized slopes are simply the centered difference $(V(I+1)-V(I-1))/2$. Note that even under this option, the monotonization routine BDOK1 is subsequently called.

PRINT

Printing of results. Reading this routine is self-explanatory. Note some features added for present CHARGE version. User is called to modify this routine to his specific needs.

SOF

Run termination when an error has been detected. ISTOP is an informative index. All printing of relevant information should be done at the calling routine prior to calling SOF. Note that the run is ended in SOF by deliberately causing a system error of computing SQRT(-1). This is done in order to trigger printing of the sequence of calling routines by the operating system.

RIEMAN

Here a single Riemann Problem (RP) is solved by calling RIEMAN from CYCEUL. Referring to Fig. A-2, the RP is solved by finding the point of intersection (USTAR,PSTAR) of Left-propagating and Right-propagating shock/rarefaction adiabats in the (U,P) plane. Prior to the actual computation, the qualitative wave structure is determined. It is characterized by the index NCASE as follows :

NCASE = 1 - Left wave is rarefaction, Right wave is shock.

NCASE = 2 - Both waves are shock.

NCASE = 3 - Left wave is shock, Right wave is rarefaction.

NCASE = 4 - Both waves are rarefaction.

The computation of (USTAR,PSTAR) is coded separately for each case. Newton-Raphson iteration is employed, the first guess being the intersection of the Left and Right rarefaction branches (or their extrapolations), which is done in closed-form. Since in a smooth flow this guess is close to the exact (USTAR,PSTAR), little extra CPU effort is spent on subsequent Newton-Raphson iterations. These are truly needed only in regions of shock wave computation.

The computation in RIEMAN is concluded by computing UW(1),...,UW(5) (UW(6)=infinity). From these wave speeds, the flux index NFLUX that denotes the location of the X-axis on the (X,T) wave diagram of the RP solution (Fig. A-3), is evaluated. It is later needed in subroutine FLUXE.

MAGA

The major purpose of this routine is to compute DUIDT and DPIDT along the contact surface of the RP solution. Since U and P are continuous across the contact, so are their time-derivatives along the contact. Thus, DUIDT and DPIDT are solved from a set of two linear equations. The coefficients of each equation are determined by GRP analysis of the wave on one side. See References 4-6 (particularly Ref. 6) for details.

FLUXE

The major task of this routine is to compute second-order fluxes. This is done in two phases. The first phase is up to statement 9 CONTINUE, where using NFLUX the X-suffixed values of flow variables and their time-derivatives are defined. An X-suffix means that the variable or its time-derivative are related to the line $X = X(I)$ on the (X, T) wave diagram (Fig. A-3). In the second phase, these variables and their time-derivatives are used to extend fluxes at $X(I)$ to Half-time-step (hence the suffix H), i.e. $T + DT/2$. It is these fluxes which are the second-order accurate fluxes for the integration of the conservation laws from T to $T + DT$. Also, cell-interface flow variables (suffix N) are extended to New time level $T + DT$. These are later used in defining cell differences $DU(I)$, $DP(I)$ and $DRO(I)$ in CYCEUL.

A.5 Listing of GRP Code

		<u>CHARGE VERSION</u>	
C\$OPTIONS LIST		CHA0001	
IMPLICIT REAL*8(A-H,0-Z,\$)		CHA0002	
C PROGRAM GRP - GENERALIZED RIEMANN PROBLEM.		CHA0003	
C EXPANSION OF A DETONATED SPHERICAL CHARGE IN VACUUM.		CHA0004	
C INITIAL CONDITIONS FROM TAYLOR'S SELF SIMILAR SOLUTION.		CHA0005	
COMMON B(102,26)		CHA0006	
1	ENDB	CHA0007	
COMMON /AB/A(50)		CHA0008	
EQUIVALENCE (L,A(1)),(LL,A(2)),(T,A(3)),(DT,A(4)),(TMAX,A(5)),		CHA0009	
1	(TMUD,A(6)),(DTMUD,A(7)),(JOB,A(8)),(NERI,A(9)),	CHA0010	
2	(JJJ,A(10)),(KEYMON,A(11)),(NCYC,A(12))	CHA0011	
EQUIVALENCE (COLELA,A(13))		CHA0012	
EQUIVALENCE (LAGEUL,A(14))		CHA0013	
EQUIVALENCE (UGAL,A(15))		CHA0014	
EQUIVALENCE (KEYEK,A(16))		CHA0015	
EQUIVALENCE (NCYCPR,A(17))		CHA0016	
EQUIVALENCE (STAB,A(18)),(DTBA,A(19)),(DTKOD,A(20)),(KDT,A(21))		CHA0017	
COMMON /MONIT/CASEAV(4),NC14(4),NF16(6),		CHA0018	
1	NMONU(4),NMONP(4),NMONRO(4),NMONZ(4)	CHA0019	
DIMENSION NZERO(26)		CHA0020	
EQUIVALENCE (NZERO(1),NC14(1))		CHA0021	
COMMON/PULS/PRESS(10),PULSE1(10),PULSE2(10),PULSE3(10),PULSE4(10)		CHA0022	
*****			CHA0023
DO 20 N=1,26		CHA0024	
20	NZERO(N)=0	CHA0025	
DO 21 N=1,4		CHA0026	
21	CASEAV(N)=0.	CHA0027	
DO 31 N=1,10		CHA0028	
PRESS(N)=0.		CHA0029	
PULSE1(N)=0.		CHA0030	
PULSE2(N)=0.		CHA0031	
PULSE3(N)=0.		CHA0032	
PULSE4(N)=0.		CHA0033	
31	CONTINUE	CHA0034	
NMAT=26		CHA0035	
C L=(LOCF(ENDB)-LOCF(B(1,1))/NMAT		CHA0036	
L=102		CHA0037	
LL=L-1		CHA0038	
NN=NMAT*L		CHA0039	
DO 1 I=1,L		CHA0040	
DO 1 II=1,NMAT		CHA0041	
1	B(I,II)=0.	CHA0042	
CALL MAIN0(L,B(1, 1),B(1, 2),B(1, 3),B(1, 4),B(1, 5),		CHA0043	
1	B(1, 6),B(1, 7),B(1, 8),B(1, 9),B(1,10),	CHA0044	
2	B(1,11),B(1,12),B(1,13),B(1,14),B(1,15),	CHA0045	
3	B(1,16),B(1,17),B(1,18),B(1,19),B(1,20),	CHA0046	
4	B(1,21),B(1,22),B(1,23),B(1,24),B(1,25),	CHA0047	
5	B(1,26))	CHA0048	
STOP		CHA0049	
END		CHA0050	
SUBROUTINE MAIN0		MAIN0	CHA0051
1	(L,X,U,P,RO,G,E,DU,DP,DRO,DG,DXSI,MIN,	CHA0052	
2	US,PS,UIDOT,PIDOT,	CHA0053	
*	FIMZ,ZMDOT,	CHA0054	
3	TENA,FIRO,FIM,FIE,GIP,VOL,Z,DZ)	CHA0055	
IMPLICIT REAL*8(A-H,0-Z,\$)		CHA0056	
DIMENSION X(L),U(L),P(L),RO(L),G(L),E(L),DU(L),DP(L),DRO(L),		CHA0057	
1	DG(L),DXSI(L),MIN(L),	CHA0058	
2	US(L),PS(L),UIDOT(L),PIDOT(L)	CHA0059	
3	,TENA(L),FIRO(L),FIM(L),FIE(L)	CHA0060	
4	,GIP(L),VOL(L),Z(L),DZ(L)	CHA0061	
5	,FIMZ(L),ZMDOT(L)	CHA0062	
COMMON /AB/A(50)		CHA0063	
EQUIVALENCE (LL,A(2)),(T,A(3)),(DT,A(4)),(TMAX,A(5)),		CHA0064	
1	(TMUD,A(6)),(DTMUD,A(7)),(JOB,A(8)),(NERI,A(9)),	CHA0065	
2	(JJJ,A(10)),(KEYMON,A(11)),(NCYC,A(12))	CHA0066	
EQUIVALENCE (LAGEUL,A(14))		CHA0067	
EQUIVALENCE (NCYCPR,A(17))		CHA0068	
EQUIVALENCE (STAB,A(18)),(DTBA,A(19)),(DTKOD,A(20)),(KDT,A(21))		CHA0069	
COMMON /TOT/AMTOT,ETOT,EKTOT,EPTOT,TENTOT		CHA0070	
*****			CHA0071
T=0.		CHA0072	

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NCYC=0          CHA0073
JJJ=0          CHA0074
CALL NETUNM    CHA0075
DELT=DT        CHA0076
CALL BEGIN     CHA0077
1              (L,X,U,P,RO,G,E,DU,DP,DRO,DG,DXSI,MIN,    CHA0078
2              US,PS,UIDOT,PIDOT,                           CHA0079
*              FIMZ,ZMDOT,                                CHA0080
3              TENA,FIRO,FIM,FIE,GIP,VOL,Z,DZ)          CHA0081
CALL SAFAE     (L,X,U,P,RO,G,E,DU,DP,DRO,DG,DXSI,MIN,    CHA0082
1              US,PS,UIDOT,PIDOT,                           CHA0083
*              FIMZ,ZMDOT,                                CHA0084
3              TENA,FIRO,FIM,FIE,GIP,VOL,Z,DZ)          CHA0085
1              NCYC=NCYC+1                               CHA0086
1              NCYC=NCYC+1                               CHA0087
C TIME STEP CONTROL.                               CHA0088
DT=DTBA        DT=DTBA                               CHA0089
IF(DT.GT.1.1D0*DTKOD.AND.DTKOD.NE.0.) DT=1.1D0*DTKOD CHA0090
IF(NCYC.EQ.2) DT=DT/10.D0                         CHA0091
IF (NCYC.EQ.1) DT=0.                               CHA0092
IF(DT.EQ.0.) GO TO 11                            CHA0093
NHAD=((TMUD-T)/DT-1.D-10)                         CHA0094
IF(NHAD.GE.10) GO TO 11                            CHA0095
DT=(TMUD-T)/DFLOAT(NHAD+1)                         CHA0096
11             CONTINUE                               CHA0097
T=T+DT        T=T+DT                               CHA0098
IF((NCYC/NCYCPR)*NCYCPR.NE.NCYC.AND.NCYC.GT.NCYCPR) GO TO 33 CHA0099
PRINT 10, NCYC,T,DT,KDT                           CHA0100
10             FORMAT(1X,'NCYC=',I4,3X,'T=',D11.4,3X,'DT=',D11.4,3X,'KDT=',I4) CHA0101
33             CONTINUE                               CHA0102
DTBA=DTMUD   DTBA=DTMUD                           CHA0103
KDT=0         KDT=0                               CHA0104
NERI=1         NERI=1                               CHA0105
IF (DABS(T-TMUD).LT.1.D-8) NERI=0                CHA0106
CALL CYCEUL   CALL CYCEUL                           CHA0107
1              (L,X,U,P,RO,G,E,DU,DP,DRO,DG,DXSI,MIN,    CHA0108
2              US,PS,UIDOT,PIDOT,                           CHA0109
*              FIMZ,ZMDOT,                                CHA0110
3              TENA,FIRO,FIM,FIE,GIP,VOL,Z,DZ)          CHA0111
CALL SAFAE     (L,X,U,P,RO,G,E,DU,DP,DRO,DG,DXSI,MIN,    CHA0112
1              US,PS,UIDOT,PIDOT,                           CHA0113
*              FIMZ,ZMDOT,                                CHA0114
3              TENA,FIRO,FIM,FIE,GIP,VOL,Z,DZ)          CHA0115
IF (NERI.NE.0) GO TO 2                            CHA0116
CALL PRINT    CALL PRINT                           CHA0117
1              (L,X,U,P,RO,G,E,DU,DP,DRO,DG,DXSI,MIN,    CHA0118
2              US,PS,UIDOT,PIDOT,                           CHA0119
*              FIMZ,ZMDOT,                                CHA0120
3              TENA,FIRO,FIM,FIE,GIP,VOL,Z,DZ)          CHA0121
IF (DABS(T-TMUD).LT.1.D-8) TMUD=TMUD+DTMUD        CHA0122
2              CONTINUE                               CHA0130
DTKOD=DT      DTKOD=DT                           CHA0131
IF (T.LT.TMAX-1.D-8) GO TO 1                      CHA0132
RETURN        RETURN                               CHA0133
END          END                                  CHA0134
SUBROUTINE NETUNM                                NETUNM      CHA0135
IMPLICIT REAL*8(A-H,O-Z,$)
COMMON /AB/A(50)
EQUIVALENCE (L,A(1))
EQUIVALENCE (LL,A(2)),(T,A(3)),(DT,A(4)),(TMAX,A(5)),    CHA0136
1              (TMUD,A(6)),(DTMUD,A(7)),(JOB,A(8)),(NERI,A(9)), CHA0137
2              (JJJ,A(10)),(KEYMON,A(11)),(NCYC,A(12))      CHA0138
EQUIVALENCE (COLELA,A(13))                         CHA0139
EQUIVALENCE (LAGEUL,A(14))                         CHA0140
EQUIVALENCE (KEYEK,A(16))                         CHA0141
EQUIVALENCE (NCYCPR,A(17))                         CHA0142
EQUIVALENCE (STAB,A(18)),(DTBA,A(19)),(DTKOD,A(20)),(KDT,A(21)) CHA0143
COMMON/DETO/QDET,PCJDET,RCJDET,UCJDET,DCJDET,P0DET,RO0DET,    CHA0144
1              RATE,TEMPC                           CHA0145
COMMON/DIFFUS/U2,P2,R02,ARW                         CHA0146
COMMON /DRAW/GODELX,GODELY,UMIN,UMAX,PMIN,PMAX,ROMIN,ROMAX CHA0147

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1      ,XMIN,XMAX,SMIN,SMAX,IVERSA          CHA0152
COMMON /GAM/GAMA,NG,MU2,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11  CHA0153
1      ,G12,G13,G14,G15,G16,G17,G18,G19,G20,G21,G22,G23  CHA0154
2      ,G24,G25,G26,G27,G28,G29,G30,G31,G32,G33,G34,G35  CHA0155
REAL*8 NG,MU2          CHA0156
NAMELIST /IN/LIN,GAMA,DT,TMUD,DTMUD,TMAX,          CHA0157
1      GODELX,GODELY,UMIN,UMAX,PMIN,PMAX,ROMIN,ROMAX,  CHA0158
2      SMIN,SMAX,IVERSA,KEYMON,COLELA,STAB  CHA0159
3      ,LAGEUL,KEYEK  CHA0160
4      ,QDET  CHA0161
*****          CHA0162
LIN=L          CHA0163
LAGEUL=2          CHA0164
NCYCPR=1          CHA0165
KEYEK=1          CHA0166
TMUD=0.          CHA0167
DTMUD=10.00          CHA0168
TMAX=100.00          CHA0169
STAB=0.5D0          CHA0170
DT=1.D-2          CHA0171
KEYMON=1          CHA0172
GAMA=3.D0+1.D-6          CHA0173
QDET=0.04D0          CHA0174
RATE=0.          CHA0175
TEMPC=1.D50          CHA0176
GODELX=16D0          CHA0177
GODELY=20.D0          CHA0178
IVERSA=100          CHA0179
UMIN=0.          CHA0180
UMAX= 1.D0          CHA0181
PMIN=0.          CHA0182
PMAX=0.5D0          CHA0183
ROMIN=0.          CHA0184
ROMAX=3.D0          CHA0185
SMIN=0.          CHA0186
SMAX=0.03D0          CHA0187
COLELA=0.          CHA0188
READ IN          CHA0189
          CHA0190
PRINT IN          CHA0191
          CHA0192
GG=2.D0*GAMA/(GAMA-1.D0)          CHA0193
NG=GG          CHA0194
CONTINUE          CHA0195
MU2=(GAMA-1.D0)/(GAMA+1.D0)          CHA0196
G1=GAMA-1.D0          CHA0197
G2=1.D0-MU2          CHA0198
G3=2.D0/(3.D0*GAMA-1.D0)          CHA0199
G4=(GAMA+1.D0)/2.D0          CHA0200
G5=0.5D0*(3.D0*GAMA-1.D0)/(GAMA+1.D0)          CHA0201
G6=(GAMA+1.D0)/(2.D0*GAMA)          CHA0202
G7=2.D0/(GAMA-1.D0)          CHA0203
G8=(GAMA-1.D0)/(2.D0*GAMA)          CHA0204
G9=(GAMA+1.D0)/(4.D0*GAMA)          CHA0205
G10=1.D0/GAMA          CHA0206
G11=(GAMA+1.D0)/4.D0          CHA0207
G12=GAMA/(GAMA-1.D0)          CHA0208
G13=0.5D0*(GAMA-3.D0)/(GAMA+1.D0)          CHA0209
G14=0.5D0*(3.D0*GAMA-5.D0)/(GAMA+1.D0)          CHA0210
G15=GAMA*(3.D0*GAMA-1.D0)          CHA0211
G16=(GAMA+1.D0)/(2.D0*(GAMA-1.D0))          CHA0212
G17=GAMA+1.D0          CHA0213
G18=GAMA*(GAMA+1.D0)/(3.D0*GAMA-1.D0)          CHA0214
G19=(3.D0*GAMA-1.D0)/(GAMA+1.D0)          CHA0215
G20=2.D0*(GAMA-1.D0)/(3.D0*GAMA-1.D0)**2          CHA0216
G21=GAMA*(3.D0*GAMA-5.D0)/(3.D0*GAMA-1.D0)**2          CHA0217
GODELX=GODELX/2.54D0          CHA0218
GODELY=GODELY/2.54D0          CHA0219
CALL NAMPLT(IVERSA)          CHA0220
CALL LIMIT(1000.D0)          CHA0221
CALL PLOT(0.,0.5D0,-3)          CHA0222
PODET=0.          CHA0223

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ROODET=0.                                              CHA0224
PCJDET=0.                                              CHA0225
UCJDET=0.                                              CHA0226
DCJDET=0.                                              CHA0227
RCJDET=0.                                              CHA0228
IF(QDET.LE.0.) GO TO 100                               CHA0229
C  DETONATION DATA                                     CHA0230
  QDET=0.04D0                                         CHA0231
  PODET=0.                                              CHA0232
  ROODET=1.8D0                                         CHA0233
  PCJDET=PODET-(GAMA-1.D0)*(-QDET)*ROODET+          CHA0234
  1  DSQRT(((GAMA-1.D0)*QDET*ROODET)**2-2.D0*MU2*GAMA*  CHA0235
  2  (-QDET)*PODET*ROODET)                           CHA0236
  RCJDET=ROODET*((GAMA+1.D0)*PCJDET-PODET)/(GAMA*PCJDET)  CHA0237
  CCJ=DSQRT(GAMA*PCJDET/RCJDET)                      CHA0238
  DCJDET=CCJ*RCJDET/ROODET                           CHA0239
  UCJDET=DCJDET-CCJ                                  CHA0240
  PRINT 101                                         CHA0241
101  FORMAT(1H1,/,1X,'DETONATION DATA')               CHA0242
  PRINT 102, QDET,GAMA,TEMPC,RATE                   CHA0243
102  FORMAT(/1X,'QDET,GAMA,TEMP,RATE=',4D18.8)       CHA0244
  PRINT 103, ROODET,PODET                           CHA0245
103  FORMAT(/1X,'UNBURNED STATE      ROODET,PODET=',2D18.8)  CHA0246
  PRINT 104, DCJDET,PCJDET,RCJDET,UCJDET            CHA0247
104  FORMAT(/1X,'CJ POINT      DCJDET,PCJDET,RCJDET,UCJDET=',4D18.8)  CHA0248
100  CONTINUE                                         CHA0249
      RETURN                                         CHA0250
      END                                             CHA0251
      SUBROUTINE BEGIN                                BEGIN      CHA0252
1           (L,X,U,P,RO,G,E,DU,DP,DRO,DG,DXSI,MIN,      CHA0253
2           US,PS,UIDOT,PIDOT,                         CHA0254
*           FIMZ,ZMDOT,                                CHA0255
3           TENA,FIRO,FIM,FIE,GIP,VOL,Z,DZ)          CHA0256
  IMPLICIT REAL*8(A-H,O-Z,$)                         CHA0257
  DIMENSION X(L),U(L),P(L),RO(L),G(L),E(L),DU(L),DP(L),DRO(L),      CHA0258
1           DG(L),DXSI(L),MIN(L),                      CHA0259
2           US(L),PS(L),UIDOT(L),PIDOT(L)            CHA0260
3           ,TENA(L),FIRO(L),FIM(L),FIE(L)          CHA0261
4           ,GIP(L),VOL(L),Z(L),DZ(L)              CHA0262
5           ,FIMZ(L),ZMDOT(L)                      CHA0263
  COMMON /AB/A(50)                                    CHA0264
  COMMON /GAM/GAMA,NG,MU2,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11  CHA0265
1           ,G12,G13,G14,G15,G16,G17,G18,G19,G20,G21,G22,G23  CHA0266
2           ,G24,G25,G26,G27,G28,G29,G30,G31,G32,G33,G34,G35  CHA0267
  REAL*8 NG,MU2                                     CHA0268
  EQUIVALENCE (LL,A(2))                           CHA0269
  EQUIVALENCE (LAGEUL,A(14))                      CHA0270
  EQUIVALENCE (UGAL,A(15))                        CHA0271
  EQUIVALENCE (STAB,A(18)),(DTBA,A(19)),(DTKOD,A(20)),(KDT,A(21))  CHA0272
  COMMON/DETO/QDET,PCJDET,RCJDET,UCJDET,DCJDET,PODET,ROODET,      CHA0273
1           RATE,TEMPC                                CHA0274
  COMMON /DRAW/GODELX,GODELY,UMIN,UMAX,PMIN,PMAX,ROMIN,ROMAX      CHA0275
1           ,XMIN,XMAX,SMIN,SMAX,IVERSA              CHA0276
  COMMON/GIT/ROLIM,ELIM,XGIT(200),ROGIT(200),ROUGIT(200),EGIT(200)  CHA0277
  COMMON /GITN/NPO                                CHA0278
  LOGICAL CSOF                                     CHA0279
*****DTBA=0.                                         *****CHA0280
  DTKOD=0.                                         CHA0281
  KDT=0.                                           CHA0282
  P0=1.D-9                                         CHA0283
  RH00=1.D-7                                         CHA0284
  U0=UCJDET                                         CHA0285
  UGAL=0.                                           CHA0286
  X0=0.                                             CHA0287
  X1=50.D0                                         CHA0288
  XCHARG=10.D0                                       CHA0289
  XMIN=X0                                         CHA0290
  XMAX=X1                                         CHA0291
  DX=(X1-X0)/(L-2.D0)                           CHA0292
  DO 1 I=2,L                                         CHA0293
  X(I)=X0+(I-2.D0)*DX                           CHA0294
1

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CONTINUE                                     CHA0296
X(L)=X1                                     CHA0297
U0=U0*CROSS(XCHARG)                         CHA0298
DO 2 I=2,LL                                  CHA0299
IF(I.GT.2) U(I)=U0/CROSS(X(I))               CHA0300
P(I)=P0                                      CHA0301
RO(I)=RH00                                    CHA0302
Z(I)=0.                                       CHA0303
GO TO (31,32), LAGEUL                      CHA0304
CONTINUE                                     CHA0305
E(I)=P(I)/((GAMA-1.D0)*RO(I))+0.5D0*U(I)**2+Z(I)*QDET CHA0306
GO TO 30                                     CHA0307
CONTINUE                                     CHA0308
E(I)=P(I)/(GAMA-1.D0)+0.5D0*RO(I)*U(I)**2+Z(I)*RO(I)*QDET CHA0309
CONTINUE                                     CHA0310
G(I)=DSQRT(GAMA*P(I)*RO(I))                 CHA0311
CONTINUE                                     CHA0312
DO 3 I=2,LL                                  CHA0313
TENA(I)=RO(I)*U(I)                          CHA0314
VOL(I)=(X(I+1)-X(I))*(X(I+1)**2+X(I+1)*X(I)+X(I)**2)/3.D0 CHA0315
CONTINUE                                     CHA0316
CH0317                                     CHA0317
INSERT DETONATED CHARGE FLOW FIELD FROM TAYLOR'S SOLUTION. CHA0318
CH0319                                     CHA0319
CALL TAYLOR(GAMA)                           CHA0320
RONORM=RCJDET                                CHA0321
RUNORM=RCJDET*UCJDET                         CHA0322
ENORM=RCJDET*DCJDET**2                      CHA0323
XLIM=XGIT(NP0)                             CHA0324
NGIT=NP0-1                                  CHA0325
XG1=XLIM                                    CHA0326
XG2=XGIT(NGIT)                            CHA0327
AROIP =ROGIT (NP0)+ROLIM*XLIM**3/3.D0      CHA0328
AROUIP=ROUGIT(NP0)                         CHA0329
AEIP  =EGIT  (NP0)+ ELIM*XLIM**3/3.D0      CHA0330
XP=X(2)/XCHARG                            CHA0331
DO 100 I=2,LL                               CHA0332
IP=I+1                                      CHA0333
XI=XP                                       CHA0334
AROI =AROIP                                 CHA0335
AROUI=AROUIP                               CHA0336
AEI  =AEIP                                 CHA0337
XP=X(IP)/XCHARG                           CHA0338
IF(DABS(XP-1.D0).LT.1.D-10) XP=1.D0       CHA0339
CSOF=(XP.GE.1.D0)                          CHA0340
IF(XP.GE.XLIM) GO TO 101                   CHA0341
UNIFORM FLOW REGION                         CHA0342
DELVOL=(XLIM-XP)*(XLIM**2+XLIM*XP+XP**2)/3.D0 CHA0343
AROIP =ROGIT (NP0)+ROLIM*DELVOL           CHA0344
AROUIP=ROUGIT(NP0)                         CHA0345
AEIP  =EGIT  (NP0)+ ELIM*DELVOL           CHA0346
GO TO 102                                  CHA0347
01 CONTINUE                                 CHA0348
NON UNIFORM FLOW REGION.                   CHA0349
IF(.NOT.CSOF) GO TO 104                   CHA0350
LAST POINT. (THIS IS THE DETONATION FRONT POINT X=1). CHA0351
AROIP= 0.                                    CHA0352
AROUIP=0.                                   CHA0353
AEIP= 0.                                    CHA0354
GO TO 102                                  CHA0355
04 CONTINUE                                 CHA0356
IF(XP.LE.XG2) GO TO 103                   CHA0357
NGIT=NGIT-1                                CHA0358
IF(NGIT.LE.0) CALL SOF('BEGIN 104. NGIT.LE.0.') CHA0359
XG1=XG2                                    CHA0360
XG2=XGIT(NGIT)                            CHA0361
GO TO 104                                  CHA0362
03 CONTINUE                                 CHA0363
FRAC=(XP-XG1)/(XG2-XG1)                   CHA0364
IF(FRAC.LT.0. ) CALL SOF('BEGIN 103. FRAC.LT.0.') CHA0365
IF(FRAC.GT.1.D0) CALL SOF('BEGIN 103. FRAC.GT.1.') CHA0366
AROIP =(1.D0-FRAC)*ROGIT (NGIT+1)+FRAC*ROGIT (NGIT) CHA0367

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AROUIP=(1.D0-FRAC)*ROUGIT(NGIT+1)+FRAC*ROUGIT(NGIT)           CHA0368
AEIP =(1.D0-FRAC)*EGIT (NGIT+1)+FRAC*EGIT (NGIT)           CHA0369
102  CONTINUE                                              CHA0370
C  COMPUTE MASS, MOMENTUM AND ENERGY DENSITIES.             CHA0371
   IF(XP.LE.XLIM) GO TO 105                                  CHA0372
C  CONSERVATION-FORM DEFINITION OF MASS, MOMENTUM AND ENERGY DENSITY.  CHA0373
   DVOL=(XP-XI)*(XP**2+XP*XI+XI**2)/3.D0                     CHA0374
   RO (I)=RONORM*(AROI - AROIP)/DVOL                         CHA0375
   TENA(I)=RUNORM*(AROUI-AROUIP)/DVOL                         CHA0376
   E  (I)=ENORM *(AEI - AEIP)/DVOL                           CHA0377
   GO TO 106                                              CHA0378
105  CONTINUE                                              CHA0379
C  UNIFORM FLOW REGION                                     CHA0380
   RO (I)=RONORM*ROLIM                         CHA0381
   TENA(I)=0.                                         CHA0382
   E  (I)=ENORM * ELIM                           CHA0383
106  CONTINUE                                              CHA0384
   U(I)=TENA(I)/RO(I)                                CHA0385
   P(I)=(GAMA-1.D0)*(E(I)-0.5D0*RO(I)*U(I)**2)          CHA0386
   PRINT 111,I,CSOF,U(I),P(I),RO(I),E(I)                CHA0387
111  FORMAT(/1X,'I,CSOF,U,P,RO,E=',I4,L3,4D14.4)          CHA0388
   IF(CSOF) GO TO 109                                  CHA0389
100  CONTINUE                                              CHA0390
109  CONTINUE                                              CHA0391
   DO 4 I=2,LL                                         CHA0392
   DXSI(I)=(X(I+1)-X(I))*RO(I)                         CHA0393
4    CONTINUE                                              CHA0394
   RETURN                                              CHA0395
   END                                              CHA0396


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SUBROUTINE TAYLOR(GAMA)                                     TAYLOR          CHA0397
IMPLICIT REAL*8(A-H,O-Z,$)                                CHA0398
C
C  TAYLOR -- SELF SIMILAR SPHERICAL DETONATION (CJ) FLOW FIELD  CHA0399
C
COMMON /GGGG/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10          CHA0400
COMMON /PAR/RH00,Q0,ROCJ,DCJ,UCJ,PCJ,DPSI,PSIMAX,C0,U0  CHA0401
COMMON /GITN/NP0                                         CHA0402
COMMON/GIT/ROLIM,ELIM,XGIT(200),ROGIT(200),ROUGIT(200),EGIT(200) CHA0403
C*****G=GAMA                                              CHA0404
PRINT 101                                              CHA0405
101  FORMAT('1')                                         CHA0406
PRINT 110                                              CHA0407
110  FORMAT(1X,'G. I. TAYLOR SOLUTION.  N,PSI,U,C,X/AM,AT,AE=//') CHA0408
   CALL INIDAT                                         CHA0409
   X=1.D0                                              CHA0410
   Y=0.                                                 CHA0411
   U=U0                                                 CHA0412
   C=C0                                                 CHA0413
   AM=0.                                                CHA0414
   AT=0.                                                CHA0415
   AE=0.                                                CHA0416
   PSI=-DLOG(U)                                         CHA0417
   DO 1 N=1,NP0                                         CHA0418
   XGIT (N)=X                                         CHA0419
   ROGIT (N)=AM                                         CHA0420
   ROUGIT(N)=AT                                         CHA0421
   EGIT  (N)=AE                                         CHA0422
   PRINT 11, N,PSI,U,C,X,AM,AT,AE                      CHA0423
11   FORMAT(1X,I4,4D14.5/5X,3D14.5)                      CHA0424
   CALL RUNGE(N,PSI,X,C,AM,AT,AE,PSIN,XN,CN,AMN,ATN,AEN) CHA0425
   PSI=PSIN                                         CHA0426
   U=DEXP(-PSI)                                         CHA0427
   X=XN                                              CHA0428
   C=CN                                              CHA0429
   AM=AMN                                         CHA0430
   AT=ATN                                         CHA0431
   AE=AEN                                         CHA0432
1    CONTINUE                                              CHA0433
   ROLIM=(C/C0)**G3                                     CHA0434
   ELIM=G5*(C/C0)**G4                                     CHA0435
   AM0=AM+(C/C0)**G3*X**3/3.D0                         CHA0436

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AM0=AM0*X. D0*(G+1.D0)/G          CHA0440
AE0=AE+(G5*(C/C0)**G4+0.5D0*(C/C0)**G3*U**2)*X**3/3.D0  CHA0441
AE0=AE0*6.D0*(G+1.D0)*(G**2-1.D0)/G          CHA0442
PRINT 22,AM0,AE0          CHA0443
22 FORMAT(///1X,'MASS AND ENERGY CHECK (SHOULD BE 1.)'//  CHA0444
1      1X,'M0=',D17.8,5X,'E0=',D17.8//)          CHA0445
1      RETURN          CHA0446
1      END          CHA0447
SUBROUTINE INIDAT          INIDAT          CHA0448
IMPLICIT REAL*8(A-H,0-Z,$)          CHA0449
COMMON /GGGG/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10          CHA0450
COMMON /PAR/RH00,Q0,ROCJ,DCJ,UCJ,PCJ,DPSI,PSIMAX,C0,U0          CHA0451
COMMON /GITN/NPO          CHA0452
*****          CHA0453
NPO=200          CHA0454
PSIMAX=10.D0          CHA0455
U0=1.D0/(G+1.D0)          CHA0456
C0=1.D0-U0          CHA0457
DPSI=PSIMAX/DFLOAT(NPO)          CHA0458
G1=G-1.D0          CHA0459
G2=G1/2.D0          CHA0460
G3=2.D0/(G-1.D0)          CHA0461
G4=2.D0*X/G/(G-1.D0)          CHA0462
G5=G/((G+1.D0)**2*(G-1.D0))          CHA0463
1      RETURN          CHA0464
1      END          CHA0465
SUBROUTINE RUNGE(N,PSI,X,C,AM,AT,AE,PSIN,XN,CN,AMN,ATN,AEN)          CHA0466
IMPLICIT REAL*8(A-H,0-Z,$)          CHA0467
COMMON /GGGG/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10          CHA0468
COMMON /PAR/RH00,Q0,ROCJ,DCJ,UCJ,PCJ,DPSI,PSIMAX,C0,U0          CHA0469
COMMON /GITN/NPO          CHA0470
*****          CHA0471
H=PSI          CHA0472
H2=H/2.D0          CHA0473
H6=H/6.D0          CHA0474
1      CALL DERIV(PSI,X,C,AM,AT,AE,          CHA0475
1      DXP1,DCDP1,DMDP1,DTDP1,DEDP1)          CHA0476
1      CALL DERIV(PSI+H2,X+H2*DXP1,C+H2*DCDP1,AM,AT,AE,          CHA0477
1      DXP2,DCDP2,DMDP2,DTDP2,DEDP2)          CHA0478
1      CALL DERIV(PSI+H2,X+H2*DXP2,C+H2*DCDP2,AM,AT,AE,          CHA0479
1      DXP3,DCDP3,DMDP3,DTDP3,DEDP3)          CHA0480
1      CALL DERIV(PSI+H,X+H*DXP3,C+H*DCDP3,AM,AT,AE,          CHA0481
1      DXP4,DCDP4,DMDP4,DTDP4,DEDP4)          CHA0482
1      PSIN=PSI+H          CHA0483
1      XN=X+H6*(DXP1+2.D0*(DXP2+DXP3)+DXP4)          CHA0484
1      CN=C+H6*(DCDP1+2.D0*(DCDP2+DCDP3)+DCDP4)          CHA0485
1      AMN=AM+H6*(DMDP1+2.D0*(DMDP2+DMDP3)+DMDP4)          CHA0486
1      ATN=AT+H6*(DTDP1+2.D0*(DTDP2+DTDP3)+DTDP4)          CHA0487
1      AEN=AE+H6*(DEDP1+2.D0*(DEDP2+DEDP3)+DEDP4)          CHA0488
1      RETURN          CHA0489
1      END          CHA0490
SUBROUTINE DERIV(PSI,X,C,AM,AT,AE,DXDP,DCDP,DMDP,DTDP,DEDP)          CHA0491
IMPLICIT REAL*8(A-H,0-Z,$)          CHA0492
COMMON /GGGG/G,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10          CHA0493
COMMON /PAR/RH00,Q0,ROCJ,DCJ,UCJ,PCJ,DPSI,PSIMAX,C0,U0          CHA0494
COMMON /GITN/NPO          CHA0495
*****          CHA0496
U=DEXP(-PSI)          CHA0497
DXDP=0.5D0*X*(C-U+X)*(C+U-X)/C**2          CHA0498
DCDP=-G2*U*(X-U)/C          CHA0499
DMDP=-(C/C0)**G3*X**2*DXDP          CHA0500
DTDP=DMDP*U          CHA0501
DEDP=-(G5*(C/C0)**G4+0.5D0*(C/C0)**G3*U**2)*X**2*DXDP          CHA0502
1      RETURN          CHA0503
1      END          CHA0504
DOUBLE PRECISION FUNCTION RATIO(X)          RATIO          CHA0505
IMPLICIT REAL*8(A-H,0-Z,$)          CHA0506
*****          CHA0507
RATIO=0.          CHA0508
IF(X.LE.1.D-8)RETURN          CHA0509
RATIO=2.D0/X          CHA0510
1      RETURN          CHA0511

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ZL=Z(IM)+0.5D0*DZ(IM)                                CHA0588
IF(ZL.GT.1.D0) ZL=1.D0                                CHA0589
IF(ZL.LT.0. ) ZL=0.                                    CHA0590
SL=PL/(G1*ROL**GAMA)                                 CHA0591
TEML=PL/ROL                                         CHA0592
UR=U(I)-0.5D0*DU(I)                                 CHA0593
PR=P(I)-0.5D0*DP(I)                                 CHA0594
ROR=R0(I)-0.5D0*DRO(I)                               CHA0595
GR=DSQRT(GAMA*PR*ROR)                               CHA0596
CR=GR/ROR                                         CHA0597
ZR=Z(I)-0.5D0*DZ(I)                                 CHA0598
IF(ZR.GT.1.D0) ZR=1.D0                               CHA0599
IF(ZR.LT.0. ) ZR=0.                                    CHA0600
SR=PR/(G1*ROR**GAMA)                               CHA0601
TEMPR=PR/ROR                                         CHA0602
CHA0603
CALL RIEMAN(L,I,MIN)                                CHA0604
CHA0605
DUDXIL=DU(IM)/DXSI(IM)                             CHA0606
DPDXIL=DP(IM)/DXSI(IM)                             CHA0607
DRDXIL=DRO(IM)/DXSI(IM)                            CHA0608
DGDXIL=0.5D0*GL*(DPDXIL/PL+DRDXIL/ROL)           CHA0609
DZDXIL=DZ(IM)/DXSI(IM)                            CHA0610
DSDXIL=SL*(DPDXIL/PL-GAMA*DRDXIL/ROL)             CHA0611
DUDXIR=DU(I)/DXSI(I)                               CHA0612
DPDXIR=DP(I)/DXSI(I)                               CHA0613
DRDXIR=DRO(I)/DXSI(I)                             CHA0614
DGDXIR=0.5D0*GR*(DPDXIR/PR+DRDXIR/ROR)           CHA0615
DZDXIR=DZ(I)/DXSI(I)                               CHA0616
DSDXIR=SR*(DPDXIR/PR-GAMA*DRDXIR/ROR)             CHA0617
SH=CROSS(X(I))                                    CHA0618
RAT=RATIO(X(I))                                    CHA0619
CHA0620
CALL MAGA(L,I,MIN)                                CHA0621
CHA0622
US(I)=USTAR                                         CHA0623
PS(I)=PSTAR                                         CHA0624
UIDOT(I)=DUIDT                                         CHA0625
PIDOT(I)=DPIDT                                         CHA0626
CHA0627
CALL FLUXE(L,I,MIN)                                CHA0628
CHA0629
FIRO(I)=FIH1                                         CHA0630
FIM (I)=FIH2                                         CHA0631
FIE (I)=FIH3                                         CHA0632
FIMZ(I)=FIH4                                         CHA0633
GIP(I)=GIH                                         CHA0634
DU(IM)=UXN-UXNM                                     CHA0635
DP(IM)=PZN-PXNM                                     CHA0636
DRO(IM)=ROXN-ROXNM                                 CHA0637
DZ(IM)=ZZN-ZXNM                                     CHA0638
CHA0639
STATIONS OUTPUT
IF((I-42)*(I-62)*(I-82)*(I-102).NE.0) GO TO 1
NPU=0
IF(I.EQ.42) NPU=1
IF(I.EQ.62) NPU=2
IF(I.EQ.82) NPU=3
IF(I.EQ.102)NPU=4
IF(NPU.EQ.0) CALL SOF('FLUXE 90. NPU.EQ.0')
PRESS(NPU)=GIH+FIH2
PULSE1(NPU)=PULSE1(NPU)+DT*GIH
PULSE2(NPU)=PULSE2(NPU)+DT*(GIH+FIH2)
PULSE3(NPU)=PULSE3(NPU)+DT*FIH1*CROSS(X(I))
PULSE4(NPU)=PULSE4(NPU)+DT*FIH2*CROSS(X(I))
CONTINUE
AMTOT=0.
ETOT=0.
EKTOT=0.
EPTOT=0.
TENTOT=0.
FI1=FIRO(2)
CHA0640
CHA0641
CHA0642
CHA0643
CHA0644
CHA0645
CHA0646
CHA0647
CHA0648
CHA0649
CHA0650
CHA0651
CHA0652
CHA0653
CHA0654
CHA0655
CHA0656
CHA0657
CHA0658
CHA0659

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      FI2=FIM (2)          CHA0660
      FI3=FIE (2)          CHA0661
      FI4=FIMZ(2)          CHA0662
      GI2=GIP(2)           CHA0663
      SH=CROSS(X(2))       CHA0664
      DO 2 I=2,LL           CHA0665
      IP=I+1                CHA0666
      FIM1=FI1                CHA0667
      FIM2=FI2                CHA0668
      FIM3=FI3                CHA0669
      FIM4=FI4                CHA0670
      GIM2=GI2                CHA0671
      SHM=SH                  CHA0672
      FI1=FIRO(IP)           CHA0673
      FI2=FIM (IP)           CHA0674
      FI3=FIE (IP)           CHA0675
      FI4=FIMZ(IP)           CHA0676
      GI2=GIP (IP)           CHA0677
      SH=CROSS(X(IP))        CHA0678
      DVOL=VOL(I)             CHA0679
      ROOLD=RO(I)             CHA0680
      POLD=P(I)                CHA0681
      EOLD=E(I)                CHA0682
      UOLD=U(I)                CHA0683
      ZOLD=Z(I)                CHA0684
      ZKODM=ZOLD*ROOLD        CHA0685
      TOLD=POLD/ROOLD         CHA0686
      DX=X(IP)-X(I)           CHA0687
      DTVOL=DT/DVOL            CHA0688
C
      RO(I)=RO(I)-DTVOL*(SH*FI1-SHM*FIM1)      CHA0690
      TENA(I)=TENA(I)-DTVOL*(SH*FI2-SHM*FIM2)-(DT/DX)*(GI2-GIM2)  CHA0691
      E(I)=E(I)-DTVOL*(SH*FI3-SHM*FIM3)      CHA0692
      U(I)=TENA(I)/RO(I)           CHA0693
      Z(I)=(ZKODM-DTVOL*(SH*FI4-SHM*FIM4))/RO(I)  CHA0694
      IF(Z(I).GT.1.D0) Z(I)=1.D0      CHA0695
      IF(Z(I).LT.0.) Z(I)=0.          CHA0696
C
      UAV=U(I)                CHA0697
      ROAV=RO(I)              CHA0698
      EP=E(I)-0.5D0*ROAV*UAV**2      CHA0700
      IF(EP.GT.0.) GO TO 291        CHA0701
      NERRP=NERRP+1              CHA0702
      ERRP=ERRP+(1.D-8-EP)*DVOL    CHA0703
      IF(ERRP.GT.0.24D0) GO TO 291  CHA0704
      EP=1.D-8                  CHA0705
291  CONTINUE                CHA0706
      IF(EP.LE.0.) GO TO 7001      CHA0707
      P(I)=G1*EP                CHA0708
      G(I)=DSQRT(GAMA*P(I)*RO(I))  CHA0709
C
      UPC=DABS(U(I))+G(I)/RO(I)    CHA0710
      DTI=STAB*DX/UPC             CHA0711
      IF(DTI.GT.DTBA) GO TO 29     CHA0712
      DTBA=DTI                  CHA0713
      KDT=I                      CHA0714
      KDT=I                      CHA0715
29   CONTINUE                CHA0716
      DXSI(I)=RO(I)*DX            CHA0717
      ETOT=ETOT+E(I)*DVOL         CHA0718
      EPTOT=EPTOT+EP*DVOl         CHA0719
      AMTOT=AMTOT+RO(I)*DVOL     CHA0720
      TENTOT=TENTOT+TENA(I)*DVOL  CHA0721
      CONTINUE                  CHA0722
      EKTOT=ETOT-EPTOT            CHA0723
C
      IF(COLELA.EQ.0.) GO TO 200  CHA0724
      CALL DCOLE(L,X,U ,DU ,MIN,1)  CHA0725
      CALL DCOLE(L,X,P,DP,MIN,2)    CHA0726
      CALL DCOLE(L,X,RO,DRO,MIN,3)  CHA0727
      CALL DCOLE(L,X,Z,DZ,MIN,4)    CHA0728
200  CONTINUE                CHA0729
      CALL BDOK1(L,X,U ,DU ,MIN,1)  CHA0730
                                         CHA0731

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CALL BDOK1(L,X,P,DP,MIN,2)                                CHA0732
CALL BDOK1(L,X,RO,DRO,MIN,3)                               CHA0733
CALL BDOK1(L,X,Z,DZ,MIN,4)                                CHA0734
PRINT 901,(NN,PRESS(NN),PULSE1(NN),PULSE2(NN),
1          PULSE3(NN)/AMTOT,PULSE4(NN)/TENTOT,NN=1,4)      CHA0735
01  FORMAT(1X,2(' ',I3,5D11.3,' '))                      CHA0736
IF(DABS(T-A(5)).LT.1.D-6) PRINT 911,NERRP,ERRP          CHA0737
11  FORMAT(//1X,'NERRP,ERRP=',I5,D15.5/)                 CHA0738
RETURN                                                 CHA0739
001 CONTINUE                                              CHA0740
PRINT 7101, I,ROAV,UAV,DRO(I),DU(I),E(I),EP,ZNEW,ZNEW-1.D0,EPI CHA0741
101 FORMAT(//1X,'FROM CYCEUL. NEGATIVE EP. IN CELL I=',I6// CHA0742
1      1X,'ROAV,UAV,DRO(I),DU(I)=' ,4D18.8//             CHA0743
2      1X,'E(I),EP,ZNEW,ZNEW-1,EPI=' ,5D14.6//             CHA0744
CALL PRINT                                              CHA0745
1          (L,X,U,P,RO,G,E,DU,DP,DRO,DG,DXSI,MIN,          CHA0746
2          US,PS,UIDOT,PIDOT,                                CHA0747
*          FIMZ,ZMDOT,                                     CHA0748
3          TENA,FIRO,FIM,FIE,GIP,VOL,Z,DZ)                 CHA0749
CALL SOF('CYCEUL 7001, NEGATIVE EP')                      CHA0750
RETURN                                                 CHA0751
END                                                   CHA0752
SUBROUTINE SAFAE                                         SAFAE   CHA0753
1          (L,X,U,P,RO,G,E,DU,DP,DRO,DG,DXSI,MIN,          CHA0754
2          US,PS,UIDOT,PIDOT,                                CHA0755
*          FIMZ,ZMDOT,                                     CHA0756
3          TENA,FIRO,FIM,FIE,GIP,VOL,Z,DZ)                 CHA0757
IMPLICIT REAL*8(A-H,O-Z,$)                                CHA0758
DIMENSION X(L),U(L),P(L),RO(L),G(L),E(L),DU(L),DP(L),DRO(L),
1          DG(L),DXSI(L),MIN(L),                                CHA0759
2          US(L),PS(L),UIDOT(L),PIDOT(L)                   CHA0760
3          ,TENA(L),FIRO(L),FIM(L),FIE(L)                 CHA0761
4          ,GIP(L),VOL(L),Z(L),DZ(L)                      CHA0762
5          ,FIMZ(L),ZMDOT(L)                                CHA0763
COMMON /AB/A(50)                                         CHA0764
EQUIVALENCE (LL,A(2)),(T,A(3)),(DT,A(4)),(NCYC,A(12)) CHA0765
EQUIVALENCE (UGAL,A(15))                                CHA0766
COMMON /GAM/GAMA,NG,MU2,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11 CHA0767
1          ,G12,G13,G14,G15,G16,G17,G18,G19,G20,G21,G22,G23 CHA0768
2          ,G24,G25,G26,G27,G28,G29,G30,G31,G32,G33,G34,G35 CHA0769
REAL*8 NG,MU2                                         CHA0770
COMMON/DETO/QDET,PCJDET,RCJDET,UCJDET,DCJDET,P0DET,RO0DET, CHA0771
1          RATE,TEMPC                                     CHA0772
COMMON/DIFFUS/U2,P2,R02,ARW                           CHA0773
***** RIGID B.C. AT I=2 *****                           CHA0774
RIGID B.C. AT I=2                                         CHA0775
U(1)=-U(2)                                              CHA0776
P(1)=P(2)                                              CHA0777
G(1)=G(2)                                              CHA0778
RO(1)=RO(2)                                             CHA0779
Z(1)=Z(2)                                              CHA0780
DU(1)=DU(2)                                             CHA0781
DP(1)=-DP(2)                                             CHA0782
DG(1)=-DG(2)                                             CHA0783
DRO(1)=-DRO(2)                                            CHA0784
DXSI(1)=DXSI(2)                                           CHA0785
***** OUTFLOW B.C. AT I=L *****                         CHA0786
OUTFLOW B.C. AT I=L                                       CHA0787
U(L)=U(LL)+DU(LL)/2.D0                                  CHA0788
P(L)=P(LL)+DP(LL)/2.D0                                  CHA0789
RO(L)=RO(LL)+DRO(LL)/2.D0                               CHA0790
G(L)=G(LL)+DG(LL)/2.D0                                  CHA0791
Z(L)=Z(LL)+DZ(LL)/2.D0                                  CHA0792
DU(L)=0.                                                 CHA0793
DP(L)=0.                                                 CHA0794
DG(L)=0.                                                 CHA0795
DRO(L)=0.                                                CHA0796
DZ(L)=0.                                                 CHA0797
DXSI(L)=DXSI(LL)                                         CHA0798

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C
RETURN
END
SUBROUTINE BDOK1(L,X,V,DV,MIN,NV)                                BDOK1
IMPLICIT REAL*8(A-H,O-Z,$)
DIMENSION X(L),V(L),DV(L),MIN(L)
COMMON /AB/A(50)
EQUIVALENCE (LL,A(2)),(KEYMON,A(11))
COMMON /DRAW/GODELX,GODELY,UMIN,UMAX,PMIN,PMAX,ROMIN,ROMAX
1           ,XMIN,XMAX,SMIN,SMAX,IVERSA
COMMON /MONIT/CASEAV(4),NC14(4),NF16(6),
1           NMONU(4),NMONP(4),NMONRO(4),NMONZ(4)
DIMENSION NMONV(4,4)
EQUIVALENCE (NMONV(1,1),NMONU(1))
DIMENSION NAMEV(4)
DATA NAMEV/'U','P','R0','Z'
DATA EPS/1.D-9/
*****                                                               CHA0821
GO TO (1,2,3,4), NV
1 AMIDA=(UMAX-UMIN)**2                                         CHA0822
GO TO 9
2 AMIDA=(PMAX-PMIN)**2                                         CHA0823
GO TO 9
3 AMIDA=(ROMAX-ROMIN)**2                                         CHA0824
GO TO 9
4 AMIDA=1.D0                                         CHA0825
GO TO 9
9 CONTINUE
AMIDA=AMIDA*EPS**2                                         CHA0826
EPSA=DSQRT(AMIDA)
DO 29 I=2,LL
ICAT=0
IF(DABS(DV(I)).LE.EPSA) DV(I)=0.
IF(DV(I).EQ.0.) GO TO 29
VLEFT=V(I)-0.5D0*DVB(I)
VRIGHT=V(I)+0.5D0*DVB(I)
VM=V(I-1)
VP=V(I+1)
SIGN=(VP-V(I))*(V(I)-VM)
IF(SIGN.GT.-AMIDA) GO TO 22
21 DV(I)=0.
ICAT=1
GO TO 20
22 CONTINUE
SIGN=(VP-VM)*DVB(I)
IF(SIGN.GT.-AMIDA) GO TO 24
23 DV(I)=0.5D0*(VP-VM)
VLEFT=V(I)-0.5D0*DVB(I)
VRIGHT=V(I)+0.5D0*DVB(I)
ICAT=2
24 SIGN=(VLEFT-VM)*DVB(I)
IF(SIGN.GT.-AMIDA) GO TO 26
25 VLEFT=VM
VRIGHT=2.D0*V(I)-VLEFT
DV(I)=VRIGHT-VLEFT
ICAT=3
26 SIGN=(VP-VRIGHT)*DVB(I)
IF (SIGN.GT.-AMIDA) GO TO 28
27 VRIGHT=VP
VLEFT=2.D0*V(I)-VRIGHT
DV(I)=VRIGHT-VLEFT
ICAT=3
28 IF(DABS(DV(I)).LE.0.5D0*DABS(VP-VM)) GO TO 31
30 DV(I)=0.5D0*(VP-VM)
ICAT=4
31 CONTINUE
20 CONTINUE
IF (DABS(DV(I)).GT.EPSA) GO TO 40
DV(I)=0.
40 CONTINUE
IF (ICAT.GT.0) NMONV(ICAT,NV)=NMONV(ICAT,NV)+1
29 CONTINUE

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RETURN                                         CHA0878
END                                           CHA0879
SUBROUTINE DCOLE(L,X,V,DV,MIN,NV)          DCOLE          CHA0880
IMPLICIT REAL*8(A-H,O-Z,$)                  CHA0881
DIMENSION X(L),V(L),DV(L),MIN(L)            CHA0882
COMMON /AB/A(50)                           CHA0883
EQUIVALENCE (LL,A(2))                      CHA0884
*****                                         CHA0885
DO 1 I=2,LL                                 CHA0886
IM=I-1                                       CHA0887
IP=I+1                                       CHA0888
DV(I)=0.5D0*(V(IP)-V(IM))                 CHA0889
CONTINUE                                     CHA0890
RETURN                                       CHA0891
END                                           CHA0892
SUBROUTINE PRINT                           PRINT          CHA0893
1      (L,X,U,P,RO,G,E,DU,DP,DRO,DG,DXSI,MIN,  CHA0894
2      US,PS,UIDOT,PIDOT,                      CHA0895
*      FIMZ,ZMDOT,                           CHA0896
3      TENA,FIRO,FIM,FIE,GIP,VOL,Z,DZ)        CHA0897
IMPLICIT REAL*8(A-H,O-Z,$)                  CHA0898
DIMENSION X(L),U(L),P(L),RO(L),G(L),E(L),DU(L),DP(L),DRO(L),  CHA0899
1      DG(L),DXSI(L),MIN(L),                   CHA0900
2      US(L),PS(L),UIDOT(L),PIDOT(L),          CHA0901
3      ,TENA(L),FIRO(L),FIM(L),FIE(L),        CHA0902
4      ,GIP(L),VOL(L),Z(L),DZ(L),             CHA0903
5      ,FIMZ(L),ZMDOT(L)                      CHA0904
COMMON /TOT/AMTOT,ETOT,EKTOT,EPTOT,TENTOT   CHA0905
COMMON /STEP0/UL,PL,ROL,GL,UR,PR,ROR,GR,USTAR,PSTAR,  CHA0906
1      RSTARL,RSTARR,GSTARL,GSTARR,          CHA0907
2      CL,CR,CSTARL,CSTARR,SL,SR,WL,WR,UWC6)  CHA0908
3      ,LAMDAL,LAMDA, RATEL,RATER,TEMPL,TEMPR,TEMPSL,TEMPSR  CHA0909
4      ,ZL,ZR,ZSTARL,ZSTARR,NFLUX,HELEML,HELEMR  CHA0910
REAL*8 LAMDAL,LAMDA                         CHA0911
LOGICAL HELEML,HELEMR                      CHA0912
COMMON /AB/A(50)                           CHA0913
EQUIVALENCE (LL,A(2)),(T,A(3)),(NCYC,A(12)),(DT,A(4))  CHA0914
EQUIVALENCE (UGAL,A(15))                   CHA0915
COMMON/DIFFUS/U2,P2,RO2,ARW                 CHA0916
COMMON/DETO/QDET,PCJDET,RCJDET,UCJDET,DCJDET,PODET,ROODET,  CHA0917
1      RATE,TEMPC                           CHA0918
COMMON /GAM/GAMA,NG,MU2,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11  CHA0919
1      ,G12,G13,G14,G15,G16,G17,G18,G19,G20,G21,G22,G23  CHA0920
2      ,G24,G25,G26,G27,G28,G29,G30,G31,G32,G33,G34,G35  CHA0921
REAL*8 NG,MU2                                CHA0922
COMMON /MONIT/CASEAV(4),NC14(4),NF16(6),  CHA0923
1      NMONU(4),NMONP(4),NMONRO(4),NMONZ(4)  CHA0924
DIMENSION CASAV1(4)                         CHA0925
LOGICAL FULLPR                            CHA0926
*****                                         CHA0927
FULLPR=.TRUE.                                CHA0928
PRINT 1                                       CHA0929
1      FORMAT(1H1)                           CHA0930
PRINT 2, T,DT,NCYC                          CHA0931
2      FORMAT(1X,10X,'RESULTS AT T=',D11.5,5X,'DT=',D11.5,5X,'NCYC=',  CHA0932
1      15//)                                CHA0933
PRINT 3, AMTOT,ETOT,EKTOT,EPTOT,TENTOT    CHA0934
3      FORMAT(1X,'AMTOT=',D20.14,2X,'ETOT,EKTOT,EPTOT=',3D22.14/  CHA0935
1      1X,'TENTOT=',D21.14//)                CHA0936
4      FORMAT(1X,' I',',',X',',',U',',',P',',',  CHA0937
1      ' RO',',',G',',',Z',',',  CHA0938
2      ' DU',',',DP',',',DRO',',',  CHA0939
3      ' DG',',',DZ')                      CHA0940
44     FORMAT(1X,' ',',',ZMDOT',',',FIMZ',',',AMDOT',',',  CHA0941
1      ' AMDOTN',',',TEMP',',',ENTALP',',',  CHA0942
2      ' AMACH',',',ENTRO',')                CHA0943
3      ' ')                                CHA0944
5      FORMAT(1X)                           CHA0945
IF (UGAL.NE.0.) PRINT 6, UGAL              CHA0946
FORMAT(/11X,'INITIAL VELOCITY CORRESPONDS TO UGAL=',D15.6/)  CHA0947
DO 10 I=1,L                                CHA0948
IF (MOD(I,10).NE.1) GO TO 11              CHA0949

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      PRINT 5
      PRINT 4
      PRINT 44
      PRINT 5
11   CONTINUE
      PRINT 12,I,X(I),U(I),P(I),RO(I),G(I),Z(I),DU(I),DP(I),DRO(I),
1           DG(I),DZ(I)
      1 FORMAT(1X,I3,6D12.5,5D11.4)
      ENTR0=P(I)/RO(I)**GAMA
      IF(.NOT.FULLPR) GO TO 131
      IF(I.EQ.1) GO TO 131
      IM=I-1
      UL=U(IM)+0.5*DU(IM)
      PL=P(IM)+0.5*DP(IM)
      ROL=RO(IM)+0.5*DRO(IM)
      GL=G(IM)+0.5*DZ(IM)
      CL=GL/ROL
      ZL=Z(IM)+0.5*DZ(IM)
      IF(ZL.LT.0.) ZL=0.
      UR=U(I)-0.5*DU(I)
      PR=P(I)-0.5*DP(I)
      GR=G(I)-0.5*DZ(I)
      ROR=RO(I)-0.5*DRO(I)
      CR=GR/ROR
      ZR=Z(I)-0.5*DZ(I)
      IF(ZR.LT.0.) ZR=0.
      IF(PL.LE.0.) PL=1.D-8
      IF(PR.LE.0.) PR=1.D-8
      CALL RIEMAN(L,I,MIN)
      XI=X(I)
      RSTAR=RSTARL
      IF(USTAR.LT.0.) RSTAR=RSTARR
      ZSTAR=ZL
      IF(USTAR.LT.0.) ZSTAR=ZR
      AMACH=USTAR/DSQRT(GAMA*PSTAR/RSTAR)
      AMDOT=RSTAR*USTAR*CROSS(XI)
      IF(I.NE.2) GO TO 132
      AMDOT0=AMDOT
      IF(DABS(AMDOT0).LT.1.D-12) AMDOT0=1.D0
132  CONTINUE
      AMDOTN=AMDOT/AMDOT0
      ENTALP=(GAMA/(GAMA-1.D0))*PSTAR/RSTAR+0.5D0*USTAR**2+QDET*ZSTAR
      ARW=1.D0
      TEMP=PSTAR/(RSTAR*ARW)
      PRINT 13,US(I),PS(I),
1           ZMDOT(I),FIMZ(I),AMDOT,AMDOTN,TEMP,ENTALP,AMACH,ENTRO
      1 FORMAT(4X,12X,5D12.5,6D11.4)
131  CONTINUE
10   CONTINUE
C   JOB STATISTICS
      DO 40 I=1,4
      CASAV1(I)=0.
      IF (NC14(I).NE.0) CASAV1(I)=CASEAV(I)/DFLOAT(NC14(I))
40   CONTINUE
      PRINT 30
30   FORMAT(///1X,10('*'),3X,'JOB STATISTICS',3X,10('*')//)
      PRINT 31,(NC14(I),I=1,4)
31   FORMAT(1X,'NO. OF VARIOUS CASES IN RIEMAN SOLVER  NC14(NCASE)=',
1           4I10)
      PRINT 301,(CASAV1(I),I=1,4)
301  FORMAT(/1X,'AVERAGE NUMBER OF ITERATIONS IN RIEMAN SOLVER',
1           1X,'  CASAV1(NCASE)=',4(F6.2,4X))
      PRINT 32,(NF16(I),I=1,6)
32   FORMAT(/1X,'NO. OF VARIOUS FLUX CASES  NF16(NFLUX)=',6I10)
      ICAT0=4
      PRINT 33,(NMONU(I),I=1,ICAT0),(NMONP(I),I=1,ICAT0),
1           (NMONRO(I),I=1,ICAT0),(NMONZ(I),I=1,ICAT0)
      1 FORMAT(/1X,'NO. OF MONOTONICITY INTERVENTIONS FOR EACH VAR.',
1           1X,'IN EACH CATEGORY.')
      1 FORMAT(1X,'NMONU (ICAT)=',4I10)
      1 FORMAT(1X,'NMONP (ICAT)=',4I10)
      1 FORMAT(1X,'NMONRO(ICAT)=',4I10)
      1 FORMAT(1X,'NMONZ(ICAT)=',4I10)

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1      1X, 'NMNZ (ICAT)=', 4I10/ )          CHA1030
      RETURN
      END
      SUBROUTINE SOF(ISTOP)                   SOF          CHA1034
      IMPLICIT REAL*8(A-H,0-Z,$)
      DIMENSION ISTOP(1)
      PRINT 1, ISTOP
      FORMAT(//1X,3H***,3X,20A4,3X,3H***//)
      PRINT 1
      XX=-1.D0
      YY=DSQRT(XX)
      STOP
      END
      SUBROUTINE RIEMAN(L,I,MIN)              RIEMAN      CHA1310
      IMPLICIT REAL*8(A-H,0-Z,$)
      DIMENSION MIN(L)
      COMMON /STEP0/UL,PL,ROL,GL,UR,PR,ROR,GR,USTAR,PSTAR,
1          RSTARL,RSTARR,GSTARL,GSTARR,          CHA1311
2          CL,CR,CSTARL,CSTARR,SL,SR,WL,WR,UW(6)  CHA1312
3          ,LAMDAL,LAMDAR,RATEL,RATER,TEMPL,TEMPLR,TEMPSL,TEMPSR  CHA1313
4          ,ZL,ZR,ZSTARL,ZSTARR,NFLUX,HELEM,HELEM
      REAL*8 LAMDAL,LAMDAR
      LOGICAL HELEM,HELEM
      COMMON /STEP1/DUIDT,DPIDT,DGIDTL,DGIDTR,DRIDTL,DRIDTR
2          ,ASTARL,ASTARR,LAMDSL,LAMDSR,DSDAL,DSDAR,DZDAL,DZDAR  CHA1320
3          ,RAT,SH
4          ,BETACL,BETACR,DSDASL,DSDASR,DZDASL,DZDASR
      REAL*8 LAMDSL,LAMDSR,DSDAL,DSDAR,DZDAL,DZDAR
      COMMON /DRAW/GODELX,GODELY,UMIN,UMAX,PMIN,PMAX,ROMIN,ROMAX
1          ,XMIN,XMAX,SMIN,SMAX,IVERSA          CHA1325
      COMMON /GAM/GAMA,NG,MU2,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11
1          ,G12,G13,G14,G15,G16,G17,G18,G19,G20,G21,G22,G23  CHA1327
2          ,G24,G25,G26,G27,G28,G29,G30,G31,G32,G33,G34,G35  CHA1328
      REAL*8 NG,MU2
      COMMON /AB/A(50)
      COMMON /MONIT/CASEAV(4),NC14(4),NF16(6),
1          NMONU(4),NMONP(4),NMONR(4),NMNZ(4)          CHA1332
***** DATA NMNZ/63/          CHA1334
***** DATA EPS/1.D-8/          CHA1335
***** DATA NTRY/0/          CHA1336
***** UW(6)=1.D20          CHA1337
***** WL=0.          CHA1338
***** WR=0.          CHA1339
      ZETAL=PL**G8
      ZETAR=PR**G8
      CLG=CL/GAMA
      CRG=CR/GAMA
      ZSTARL=ZL
      ZSTARR=ZR
      IF (ZETAL.LT.ZETAR) GO TO 102
      LEFT PRESSURE IS HIGHER
01  CONTINUE
      EVERR=(PL-PR)/PR
      USR=UR+CRG*EVERR/DSQRT(1.D0+G6*EVERR)
      SRR=USR
      UEL=UL-G7*CL*(ZETAR-ZETAL)/ZETAL
      SLL=UEL
      NL=2
      NR=2
      IF (USR.GE.UL) NL=1
      IF (UEL.LE.UR) NR=1
      IF (DABS(EVERR).LT.EPS) GO TO 100
      IF (NL.EQ.2.AND.NR.EQ.1) GO TO 7001
      GO TO 100
      RIGHT PRESSURE IS HIGHER
02  CONTINUE
      EVERL=(PR-PL)/PL
      USL=UL-CLG*EVERL/DSQRT(1.D0+G6*EVERL)
      SLL=USL
      UER=UR+G7*CR*(ZETAL-ZETAR)/ZETAR

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SRR=UER                                     CHA1369
NL=2                                         CHA1370
NR=2                                         CHA1371
IF (UER.GE.UL) NL=1                         CHA1372
IF (USL.LE.UR) NR=1                         CHA1373
IF (DABS(EVERL).LT.EPS) GO TO 100          CHA1374
IF (NL.EQ.1.AND.NR.EQ.2) GO TO 7001        CHA1375
GO TO 100                                     CHA1376
100  CONTINUE                                  CHA1377
IF (NL.EQ.1.AND.NR.EQ.2) NCASE=1           CHA1378
IF (NL.EQ.2.AND.NR.EQ.2) NCASE=2           CHA1379
IF (NL.EQ.2.AND.NR.EQ.1) NCASE=3           CHA1380
IF (NL.EQ.1.AND.NR.EQ.1) NCASE=4           CHA1381
IF(DABS(PL-PR)+DABS(UL-UR).LT.EPS*(PMAX-UMIN)) NCASE=4 CHA1382
UMIDA=EPS*DMAX1(CL,CR)                      CHA1383
DUDZL=-G7*CL/ZETAL                         CHA1384
DUDZR= G7*CR/ZETAR                         CHA1385
ZETA=-(UR-UL)+ZETAR*DUDZR-ZETAL*DUDZL) / (DUDZR-DUDZL) CHA1386
IF (ZETA.LE.0.) GO TO 7002                  CHA1387
N=0                                         CHA1388
GO TO (1,2,3,4), NCASE                      CHA1389
C THE CASE ES                               CHA1390
1  ITYPE=NCASE                               CHA1391
HELEM1=.FALSE.                               CHA1392
HELEM2=.TRUE.                                CHA1393
11  N=N+1                                    CHA1394
IF (N.GT.NMAX) GO TO 7003                  CHA1395
ZETAF=ZETA                                   CHA1396
UEL =UL-G7*CL*(ZETAF-ZETAL)/ZETAL          CHA1397
PPR=(ZETAF/ZETAR)**NG                      CHA1398
EVERR=PPR-1.D0                                CHA1399
SQRR=DSQRT(1.D0+G6*EVERR)                  CHA1400
USR=UR+CRG*EVERR/SQRR                      CHA1401
DU=UEL-USR                                  CHA1402
IF (DABS(DU).LE.UMIDA) GO TO 10             CHA1403
DUDZR=NG*CRG*(PPR/ZETAF)*(1.D0+G9*EVERR)/SQRR**3 CHA1404
ZETA=ZETAF+DU/(DUDZR-DUDZL)                 CHA1405
GO TO 11                                     CHA1406
10  CONTINUE                                  CHA1407
USTAR=(UEL+USR)/2.D0                         CHA1408
IF(DABS(USTAR).LT.EPS*UMAX) USTAR=0.        CHA1409
PSTAR=PPR*PR                                 CHA1410
CSTARL=CL+(UL-USTAR)/G7                      CHA1411
RSTARL=GAMA*PSTAR/CSTARL**2                  CHA1412
GSTARL=CSTARL*RSTARL                         CHA1413
C EQU. NO. 69.01 OF THE BOOK BY COURANT-FRIEDRICH.  CHA1414
WWR=G11*(USTAR-UR)*ROR                      CHA1415
WR=WWR+DSQRT(GR**2+WWR**2)                  CHA1416
RSTARR=ROR*WR/(WR-ROR*(USTAR-UR))          CHA1417
GSTARR=DSQRT(GAMA*PSTAR*RSTARR)             CHA1418
CSTAR=GSTARR/RSTARR                         CHA1419
WRE=WR/ROR+UR                                CHA1420
UW(1)=UL-CL                                  CHA1421
UW(2)=USTAR-CSTARL                         CHA1422
UW(3)=USTAR                                  CHA1423
UW(4)=WRE                                    CHA1424
UW(5)=WRE                                  CHA1425
GO TO 5                                     CHA1426
C THE CASE SS                               CHA1427
2  ITYPE=NCASE                               CHA1428
HELEM1=.TRUE.                                CHA1429
HELEM2=.TRUE.                                CHA1430
21  N=N+1                                    CHA1431
IF (N.GT.NMAX) GO TO 7003                  CHA1432
ZETAF=ZETA                                   CHA1433
PF=ZETAF**NG                                CHA1434
PPL=PF/PL                                   CHA1435
PPR=PF/PR                                   CHA1436
EVERL=PPL-1.D0                                CHA1437
EVERR=PPR-1.D0                                CHA1438
SQRL=DSQRT(1.D0+G6*EVERL)                  CHA1439
SQRR=DSQRT(1.D0+G6*EVERR)                  CHA1440

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USL=UL-CLG*EVERL/SQRL          CHA1441
USR=UR+CRG*EVERR/SQRR          CHA1442
DU=USL-USR                      CHA1443
IF (DABS(DU).LE.UMIDA) GO TO 20  CHA1444
DUDZL=-NG*CLG*(PPL/ZETAf)*(1.D0+G9*EVERL)/SQRL**3  CHA1445
DUDZR= NG*CRG*(PPR/ZETAf)*(1.D0+G9*EVERR)/SQRR**3  CHA1446
ZETA=ZETAf+DU/(DUDZR-DUDZL)    CHA1447
GO TO 21                          CHA1448
CONTINUE                          CHA1449
USTAR=(USL+USR)/2.D0            CHA1450
IF(DABS(USTAR).LT.EPS*UMAX) USTAR=0.          CHA1451
PSTAR=(PPL*PL+PPR*PR)/2.D0          CHA1452
WWR=G11*(USTAR-UR)*ROR          CHA1453
WR=WWR+DSQRT(GR**2+WWR**2)        CHA1454
WWL=-G11*(USTAR-UL)*ROL          CHA1455
WL=WWL+DSQRT(GL**2+WWL**2)        CHA1456
RSTARL=ROL*WL/(WL+ROL*(USTAR-UL))        CHA1457
RSTARR=ROR*WR/(WR-ROR*(USTAR-UR))        CHA1458
GSTARL=DSQRT(GAMA*PSTAR*RSTARL)          CHA1459
GSTARR=DSQRT(GAMA*PSTAR*RSTARR)          CHA1460
CSTARL=GSTARL/RSTARL                CHA1461
CSTAR=GSTARR/RSTARR                CHA1462
WLE=-WL/ROL+UL                    CHA1463
WRE=WR/ROR+UR                    CHA1464
UW(1)=WLE                         CHA1465
UW(2)=WLE                         CHA1466
UW(3)=USTAR                       CHA1467
UW(4)=WRE                         CHA1468
UW(5)=WRE                         CHA1469
GO TO 5                           CHA1470
THE CASE SE
ITYPE=NCASE                      CHA1471
HELEM= .TRUE.                      CHA1472
HELEM= .FALSE.                     CHA1473
HELEM= .FALSE.                     CHA1474
N=N+1                            CHA1475
IF (N.GT.NMAX) GO TO 7003          CHA1476
ZETAf=ZETA                         CHA1477
UER=UR+G7*CR*(ZETAf-ZETAR)/ZETAR  CHA1478
PPL=(ZETAf/ZETAL)**NG             CHA1479
EVERL=PPL-1.D0                     CHA1480
SQRL=DSQRT(1.D0+G6*EVERL)          CHA1481
USL=UL-CLG*EVERL/SQRL             CHA1482
DU=USL-UER                         CHA1483
IF (DABS(DU).LE.UMIDA) GO TO 30  CHA1484
DUDZL=-NG*CLG*(PPL/ZETAf)*(1.D0+G9*EVERL)/SQRL**3  CHA1485
ZETA=ZETAf+DU/(DUDZR-DUDZL)    CHA1486
GO TO 31                          CHA1487
CONTINUE                          CHA1488
USTAR=(USL+UER)/2.D0            CHA1489
IF(DABS(USTAR).LT.EPS*UMAX) USTAR=0.          CHA1490
PSTAR=PPL*PL                      CHA1491
CSTAR=CR-(UR-USTAR)/G7            CHA1492
RSTARR=GAMA*PSTAR/CSTAR**2        CHA1493
GSTARR=CSTAR*RSTARR              CHA1494
WWL=-G11*(USTAR-UL)*ROL          CHA1495
WL=WWL+DSQRT(GL**2+WWL**2)        CHA1496
WLE=-WL/ROL+UL                    CHA1497
RSTARL=ROL*WL/(WL+ROL*(USTAR-UL))        CHA1498
GSTARL=DSQRT(GAMA*PSTAR*RSTARL)          CHA1499
CSTARL=GSTARL/RSTARL                CHA1500
UW(1)=WLE                         CHA1501
UW(2)=WLE                         CHA1502
UW(3)=USTAR                       CHA1503
UW(4)=USTAR+CSTAR                CHA1504
UW(5)=UR+CR                        CHA1505
GO TO 5                           CHA1506
THE CASE EE
ITYPE=NCASE                      CHA1507
HELEM= .FALSE.                     CHA1508
HELEM= .FALSE.                     CHA1509
HELEM= .FALSE.                     CHA1510
PSTAR=ZETA**NG                    CHA1511
USTAR=UL-G7*CL*(ZETA-ZETAL)/ZETAL  CHA1512

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IF(DABS(USTAR).LT.EPS*UMAX) USTAR=0.          CHA1513
CSTARL=CL+(UL-USTAR)/G7                      CHA1514
CSTARR=CR-(UR-USTAR)/G7                      CHA1515
RSTARL=GAMA*PSTAR/CSTARL**2                  CHA1516
RSTARR=GAMA*PSTAR/CSTARR**2                  CHA1517
GSTARL=RSTARL*CSTARL                         CHA1518
GSTARR=RSTARR*CSTARR                         CHA1519
UW(1)=UL-CL                                  CHA1520
UW(2)=USTAR-CSTARL                         CHA1521
UW(3)=USTAR                                  CHA1522
UW(4)=USTAR+CSTARR                         CHA1523
UW(5)=UR+CR                                  CHA1524
N=1                                         CHA1525
GO TO 5                                     CHA1526
5  CONTINUE
DO 6 K=1,6
NFLUX=K
IF (UW(K).GE.0.) GO TO 61
6  CONTINUE
NFLUX=6
61  CONTINUE
NC14(NCASE)=NC14(NCASE)+1
CASEAV(NCASE)=CASEAV(NCASE)+DFLOAT(N)
NF16(NFLUX)=NF16(NFLUX)+1
IF(NTRY.GE.2)GO TO 666
IF(I.NE.2.AND.I.NE.L) GO TO 666
PRINT 667,I,NFLUX,NCASE,PL,UL,ROL,PR,UR,ROR,USTAR,PSTAR,RSTARL,
1           RSTARR,(KK,UW(KK),KK=1,6)          CHA1543
667 1 FORMAT(/1X,'I,NFLUX,NCASE=',3I5/1X,'PL,UL,ROL,PR,UR,ROR=',6D12.4/ CHA1544
1           1X,'USTAR,PSTAR,RSTARL,RSTARR=',4D13.4/ CHA1545
2           1X,'KK,UW(KK)=',6(I4,2X,D13.4)/) CHA1546
NTRY=NTRY+1
666 CONTINUE
RETURN
7001 CONTINUE
PRINT 7101, PL,UL,PR,UR,ZETAL,ZETAR,SLL,SRR,NL,NR,I          CHA1550
7101 FORMAT(//1X,'FROM RIEMAN. AN IMPOSSIBLE CASE OF EXPANSION/SHOCK' CHA1551
1           //1X,'PL,UL,PR,UR=',4D25.14// CHA1552
2           1X,'ZETAL,ZETAR,SLL,SRR=',4D25.14// CHA1553
3           1X,'NL,NR,I=',3I10//) CHA1554
CALL SOF('7001')
7002 CONTINUE
PRINT 7102, ZETA,DUDZL,DUDZR,ZETAL,ZETAR,PL,UL,PR,UR,N,NCASE,I CHA1558
7102 FORMAT(//1X,'FROM RIEMAN. NEGATIVE PRESSURE AT THE INTERSECTION',CH
1           1X,'OF L AND R EXPANSION BRANCHES'// CHA1560
2           1X,'IT MEANS THAT A CAVITATION TENDS TO FORM. THIS', CHA1561
3           1X,'POSSIBILITY IS EXCLUDED IN PRESENT VERSION'// CHA1562
4           1X,'ZETA,DUDZL,DUDZR,ZETAL,ZETAR,PL,UL,PR,UR=',9D10.3// CHA1563
5           1X,'N,NCASE,I=',3I10//) CHA1564
CALL SOF('7002')
7003 CONTINUE
PRINT 7103, I,N,NCASE,DU,UMIDA,EPS,PL,UL,PR,UR,
1           ZETA,ZETAF,ZETAL,ZETAR,DUDZL,DUDZR          CHA1567
7103 FORMAT(//1X,'FROM RIEMAN. NUMBER OF ITERATIONS EXCEEDED.'// CHA1568
1           1X,'I,N,NCASE,DU,UMIDA,EPS=',3I6,3D18.6// CHA1569
2           1X,'PL,UL,PR,UR,ZETA,ZETAF=',6D18.10// CHA1570
3           1X,'ZETAL,ZETAR,DUDZL,DUDZR=',4D18.10//) CHA1571
CALL SOF('7003')
RETURN
END
C$OPTIONS LIST
SUBROUTINE MAGA(L,I,MIN)          MAGA          CHA1576
IMPLICIT REAL*8(A-H,O-Z,$)
DIMENSION MIN(L)
COMMON /GAM/GAMA,NG,MU2,G1,G2,G3,G4,G5,G6,G7,G8,G9,G10,G11
1           ,G12,G13,G14,G15,G16,G17,G18,G19,G20,G21,G22,G23      CHA1580
2           ,G24,G25,G26,G27,G28,G29,G30,G31,G32,G33,G34,G35      CHA1581
REAL*8 NG,MU2
COMMON/DETO/QDET,PCJDET,RCJDET,UCJDET,DCJDET,PODET,RO0DET,
1           RATE,TEMPC          CHA1582
COMMON /STEP0/UL,PL,ROL,GL,UR,PR,ROR,GR,USTAR,PSTAR,
1           RSTARL,RSTARR,GSTARL,GSTARR,          CHA1583

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2           CL,CR,CSTARL,CSTARR,SL,SR,WL,WR,UW(6)          CHA1588
3           ,LAMDAL,LAMDAR,RATEL,RATER,TEMLP,TEMPR,TEMPSL,TEMPSR  CHA1589
4           ,ZL,ZR,ZSTARL,ZSTARR,NFLUX,HELEM,HELEM             CHA1590
REAL*8 LAMDAL,LAMDAR                                         CHA1591
LOGICAL HELEM,HELEM             CHA1592
COMMON /STEP1/ DUIDT,DPIDT,DGIDTL,DGIDTR,DRIDTL,DRIDTR  CHA1593
2 ,ASTARL,ASTARR,LAMDSL,LAMDSR,DSDAL,DSDAR,DZDAL,DZDAR  CHA1594
3 ,RAT,SH                                         CHA1595
4 ,BETACL,BETACR,DSDASL,DSDASR,DZDASL,DZDASR          CHA1596
REAL*8 LAMDSL,LAMDSR,DSDAL,DSDAR,DZDAL,DZDAR          CHA1597
COMMON /GRADS/ DUDXIL,DPDXIL,DGDXIL,DRDXIL,DZDXIL,DSDXIL,  CHA1598
1           DUDXIR,DPDXIR,DGDXIR,DRDXIR,DZDXIR,DSDXIR      CHA1599
COMMON /AB/A(50)                                         CHA1600
REAL*8 LU,LP,LRO,LLAMDA                                     CHA1601
DATA EPS/1.D-6/                                         CHA1602
*****WE HERE SOLVE FOR THE TIME-DERIVATIVES ALONG THE CONTACT SURFACE, CHA1603
WE HERE SOLVE FOR THE TIME-DERIVATIVES ALONG THE CONTACT SURFACE, CHA1604
NAMELY DUIDT,DPIDT. FROM THESE WE ALSO OBTAIN THE OTHER           CHA1605
TIME-DERIVATIVES (SEE COMMON /STEP1/).           CHA1606
WE COMPUTE THE COEFFICIENTS FOR TWO EQUATIONS FOR DUIDT,DPIDT. THESE CHA1607
ARE          AAL*DUIDT+BBL*DPIDT=DDL                      CHA1608
          AAR*DUIDT+BBL*DPIDT=DDR                      CHA1609
*****IF(SH.LE.EPS)RAT=0.                                         CHA1610
IF(SH.LE.EPS)RAT=0.                                         CHA1611
                                         CHA1612
LEFT SIDE OF CONTACT                                         CHA1613
                                         CHA1614
11 IF (.NOT.HELEM) GO TO 12                                     CHA1615
11 CONTINUE                                         CHA1616
LEFT SHOCK                                         CHA1617
DP=PSTAR-PL                                         CHA1618
DU=USTAR-UL                                         CHA1619
Z2=0.5D0/(PSTAR+MU2*PL)                           CHA1620
LU=DUX*(0.5D0*ROL+MU2*Z2*GL**2)-GL**2/WL-WL      CHA1621
LRO=-0.5D0*DP/ROL                                     CHA1622
LP=-2.D0-MU2*Z2*DP                                     CHA1623
AAL=2.D0-Z2*DP                                         CHA1624
BBL=Z2*DU+WL/GSTARL**2+1.D0/WL                      CHA1625
DDL=LU*DUDXIL+LRO*DRDXIL+LP*DPDXIL                  CHA1626
DDL=DDL-WL*USTAR*RAT/RSTARL                         CHA1627
1 +UL*RAT*(-GAMA*PL/WL+DU*(GAMA*PL*MU2*Z2+0.5D0))  CHA1628
GO TO 10                                         CHA1629
12 CONTINUE                                         CHA1630
LEFT RAREFACTION                                         CHA1631
A1=DUDXIL+DPDXIL/GL                                     CHA1632
BETA=GSTARL/GL                                         CHA1633
SQB=DSQRT(BETA)                                         CHA1634
ASTARL=A1-(CL/(G15*SL))*DSDXIL*(BETA**G5-1.D0)      CHA1635
AAL=1.D0                                         CHA1636
BBL=1.D0/GSTARL                                         CHA1637
DDL=-GSTARL*ASTARL/SQB                                 CHA1638
DSDAL=DSDXIL                                         CHA1639
DZDAL=DZDXIL                                         CHA1640
DSdasl=DSDXIL*SQB                                     CHA1641
DZDASL=DZDXIL*SQB                                     CHA1642
GEOM=RAT*((GAMA-1.D0)*UL+2.D0*CL)*  CHA1643
1 (BETA**G13-1.D0)/(ROL*(GAMA-3.D0))                CHA1644
1 -4.D0*RAT*CL*(BETA**G14-1.D0)/(ROL*(3.D0*GAMA-5.D0))  CHA1645
ASTARL=ASTARL-GEOM                                     CHA1646
EVER1= GSTARL*GEOM/SQB                                CHA1647
EVER2=-RAT*USTAR*CSTARL                            CHA1648
DDL=DDL+EVER1+EVER2                                 CHA1649
GO TO 10                                         CHA1650
10 CONTINUE                                         CHA1651
                                         CHA1652
RIGHT SIDE OF CONTACT                                         CHA1653
                                         CHA1654
21 IF (.NOT.HELEM) GO TO 22                                     CHA1655
21 CONTINUE                                         CHA1656
RIGHT SHOCK                                         CHA1657
DP=PSTAR-PR                                         CHA1658
DU=USTAR-UR                                         CHA1659

```



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GO TO (1,2,3,4,5,6),NFLUX          CHA1732
CONTINUE                           CHA1733
                                   CHA1734
NFLUX=1.   LINE X=0 IS TO THE LEFT OF LEFT WAVE.      CHA1735
                                                 CHA1736
UX=UL                           CHA1737
PX=PL                           CHA1738
ROX=ROL                          CHA1739
ZX=ZL                           CHA1740
GX=GL                           CHA1741
DUDXIX=DUDXIL                   CHA1742
DPDXIX=DPDXIL                   CHA1743
DRDXIX=DRDXIL                   CHA1744
DZDXIX=DZDXIL                   CHA1745
DUDTX=-DPDXIL                   CHA1746
DRODTX=-ROL**2*DUDXIL          CHA1747
DPDTX=-GL**2*DUDXIL          CHA1748
DRODTX=DRODTX-RAT*ROL*UL      CHA1749
DPDTX=DRODTX*CL**2            CHA1750
DZDTX=0.                         CHA1751
GO TO 9                          CHA1752
CONTINUE                         CHA1753
                                 CHA1754
NFLUX=6.   LINE X=0 IS TO THE RIGHT OF RIGHT WAVE.      CHA1755
                                                 CHA1756
UX=UR                           CHA1757
PX=PR                           CHA1758
ROX=ROR                          CHA1759
ZX=ZR                           CHA1760
GX=GR                           CHA1761
DUDXIX=DUDXIR                   CHA1762
DPDXIX=DPDXIR                   CHA1763
DRDXIX=DRDXIR                   CHA1764
DZDXIX=DZDXIR                   CHA1765
DUDTX=-DPDXIR                   CHA1766
DPDTX=-GR**2*DUDXIR          CHA1767
DRODTX=-ROR**2*DUDXIR          CHA1768
DRODTX=DRODTX-RAT*ROR*UR      CHA1769
DPDTX=DRODTX*CR**2            CHA1770
DZDTX=0.                         CHA1771
GO TO 9                          CHA1772
CONTINUE                         CHA1773
                                 CHA1774
NFLUX=2.   SONIC CASE (LEFT).          CHA1775
                                                 CHA1776
BETA0=(MU2*(UL/CL+G7))**1.0/MU2      CHA1777
SQB0=DSQRT(BETA0)                   CHA1778
A1=DUDXIL+DPDXIL/GL                CHA1779
A0=A1-(CL/(G15*SL))*DSDXIL*(BETA0**G5-1.0)      CHA1780
EVER1=-((GAMA-1.0)*UL+2.0*CL)*(BETA0**G13-1.0)/(GAMA-3.0)  CHA1781
EVER2=4.0*CL*(BETA0**G14-1.0)/(3.0*GAMA-5.0)      CHA1782
EVER=(EVER1+EVER2)*RAT/ROL          CHA1783
A0=(A0+EVER)                      CHA1784
DPDAX=GL*BETA0*A0                  CHA1785
C0=MU2*(UL+G7*CL)                  CHA1786
IF(C0.LT.0.) CALL SOF('FLUXE 2.  C0 NEGATIVE.')  CHA1787
UX=C0                           CHA1788
ROX=GL*BETA0/C0                  CHA1789
ZX=ZL                           CHA1790
PX=ROX*C0**2/GAMA                CHA1791
GX=ROX*C0                        CHA1792
DPDAX=DPDAX+RAT*UX*C0*SQB0      CHA1793
DUDBX=-CL*BETA0*(-1.0/G4)/G4    CHA1794
DPDBX=PL*BETA0**MU2/G6          CHA1795
DRODBX=ROL*BETA0*(-MU2)/G4      CHA1796
DSDAX=SQB0*DSDAL                 CHA1797
DZDAX=SQB0*DZDAL                 CHA1798
DRODAX=DPDAX/C0**2-(ROX/(GAMA*SL))*DSDAX      CHA1799
DUDAX=A0                         CHA1800
DGDAX=0.5D0*GAMA*(PX*DRODAX+ROX*DPDAX)/GX    CHA1801
GO TO 9                          CHA1802
CONTINUE                         CHA1803

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FILE: CHARGE.FORTRAN A1

```

C NFLUX=5. SONIC CASE (RIGHT).
C
C BETA0=(MU2*(-UR/CR+G7))**(1.D0/MU2)
C SQB0=DSQRT(BETA0)
C A1=DUDXIR-DPDXIR/GR
C A0=A1+(CCR/(G15*SR))*DSDXIR*(BETA0**G5-1.D0)
C EVER1=(-(GAMA-1.D0)*UR+2.D0*CR)*(BETA0**G13-1.D0)/(GAMA-3.D0)
C EVER2=-4.D0*CR*(BETA0**G14-1.D0)/(3.D0*GAMA-5.D0)
C EVER=(EVER1+EVER2)*RAT/R0R
C A0=(A0+EVER)
C DPDAX=-GR*BETA0*A0
C C0=MU2*(-UR+G7*CR)
C IF(C0.LT.0.) CALL SOF('FLUXE 5. C0 NEGATIVE.')
C UX=-C0
C ROX=GR*BETA0/C0
C ZX=ZR
C PX=ROX*C0**2/GAMA
C GX=ROX*C0
C DPDAX=DPDAX-RAT*UX*C0*DSQRT(BETA0)
C DUDBX=CR*BETA0**(-1.D0/G4)/G4
C DPDBX=PR*BETA0**MU2/G6
C DRODBX=R0R*BETA0**(-MU2)/G4
C DSDAX=SQB0*DSDAR
C DZDAX=SQB0*DZDAR
C DRODAX=DPDAX/C0**2-(ROX/(GAMA*SR))*DSDAX
C DUDAX=A0
C DGDAX=0.5D0*GAMA*(PX*DRODAX+ROX*DPDAX)/GX
C GO TO 9
C 3 CONTINUE
C
C NFLUX=3. LINE X=0 IS BETWEEN THE LEFT WAVE AND THE CONTACT.
C
C UX=USTAR
C PX=PSTAR
C ROX=RSTARL
C ZX=ZL
C GX=GSTARL
C DUDXIX=-DPIDT/GSTARL**2
C DPDXIX=-DUIDT
C DUDXIX=DUDXIX-RAT*USTAR/RSTARL
C DZDXIX=DZDXIL
C DZDTX=0.
C IF (.NOT. HELEM1) GO TO 32
C 31 CONTINUE
C
C LEFT SHOCK.
C DRDXIX=(RSTARL/WL)**2*(3.D0*DUIDT
C 1 +DPIDT*(1.D0+3.D0*(WL/GSTARL)**2)/WL
C 2 +DUDXIL*WL*((GL/WL)**2+3.D0)+3.D0*DPDXIL
C 3 +DRDXIL*(WL/ROL)**2)
C EVER1=UL*RSTARL**2*RAT*((GL/WL)**2+1.D0)/(ROL*WL)
C EVER2=2.D0*RSTARL*USTAR*RAT/WL
C DRDXIX=DRDXIX+EVER1+EVER2
C DRODTX=-DUDXIX*ROX**2
C GO TO 33
C 32 CONTINUE
C BETA=GSTARL/GL
C SQB=DSQRT(BETA)
C DPDA=ASTARL*GSTARL
C DPDA=GSTARL*(ASTARL+RAT*USTAR*CSTARL/(GL*SQB))
C G41=1.D0/G4+0.5D0
C DRODA=(DRDXIL-DPDXIL/(CL*CL))*BETA**G41+DPDA/(CSTARL**2)
C DRDXIX= DRODA/SQB+DPIDT/(GSTARL*CSTARL**2)
C DRODA=DPDA/CSTARL**2-(RSTARL/(GAMA*SL))*DSDASL
C DZDTX=-DUDXIX*ROX**2
C DRDXIX=DRODA/SQB+DRODTX/GSTARL
C 33 CONTINUE
C DUDTX=DUIDT
C DPDTX=DPIDT
C GO TO 9
C 4 CONTINUE

```

NFLUX=4. LINE X=0 IS BETWEEN THE CONTACT AND THE RIGHT WAVE. CHA1876
 DPDIXI=-DUIDT CHA1877
 UX=USTAR CHA1878
 PX=PSTAR CHA1879
 ROX=RSTAR CHA1880
 ZX=ZR CHA1881
 GX=GSTARR CHA1882
 DUDXIX=-DPIDT/GSTARR**2 CHA1883
 DUDXIX=DUDXIX-RAT*USTAR/RSTAR CHA1884
 DPDIXI=-DUIDT CHA1885
 DZDXIX=DZDXIL CHA1886
 DZDTX=0. CHA1887
 IF (.NOT. HELEM) GO TO 42 CHA1888
 41 CONTINUE CHA1889
 RIGHT SHOCK CHA1890
 DRDXIX=(RSTAR/WR)**2*(3.*DUIDT CHA1891
 1 -DPIDT*(1.D0+3.D0*(WR/GSTARR)**2)/WR CHA1892
 2 -DUDXIR*WR*((GR/WR)**2+3.D0)+3.D0*DPDXIR CHA1893
 3 +DRDXIR*(WR/ROR)**2) CHA1894
 EVER1=UR*RSTAR**2*RAT*((GR/WR)**2+1.D0)/(ROR*WR) CHA1895
 EVER2=2.D0*RSTAR*USTAR*RAT/WR CHA1896
 DRDXIX=DRDXIX-EVER1-EVER2 CHA1897
 DRODTX=-DUDXIX*ROX**2 CHA1898
 GO TO 43 CHA1899
 42 CONTINUE CHA1900
 RIGHT RAREFACTION CHA1901
 BETA=GSTARR/GR CHA1902
 SQB=DSQRT(BETA) CHA1903
 DPDA=-ASTARR*GSTARR CHA1904
 DPDA=-GSTARR*(ASTARR+RAT*USTAR*CSTAR/(GR*SQB)) CHA1905
 G41=1.D0/G4+0.5D0 CHA1906
 DRODA=(DRDXIR-DPDXIR/(CR*CR)) *BETA**G41+DPDA/(CSTAR**2) CHA1907
 DRDXIX= DRODA/SQB-DPIDT/(GSTARR*CSTAR**2) CHA1908
 DRODA=DPDA/CSTAR**2-(RSTAR/(GAMA*SR))*DSDASR CHA1909
 DRODTX=-DUDXIX*ROX**2 CHA1910
 DRDXIX=DRODA/SQB-DRODTX/GSTAR CHA1911
 43 CONTINUE CHA1912
 DUDTX=DUIDT CHA1913
 DPDTX=DPIDT CHA1914
 GO TO 9 CHA1915
 9 CONTINUE CHA1916
 ***** CHA1917
 FLUXES CENTERED AT TIME T(N+1/2) AT EULERIAN POINT X=X(I). CHA1918
 ***** CHA1919
 ***** CHA1920
 FI1=ROX*UX CHA1921
 FI2=ROX*UX**2+PX CHA1922
 FI2=FI2-PX CHA1923
 FI3=UX*(G12*PX+0.5D0*ROX*UX**2) CHA1924
 FI4=ZX*ROX*UX CHA1925
 FI3=FI3+QDET*FI4 CHA1926
 ROU00=ROX*UX CHA1927
 GO TO(10,20,30,40,50,60), NFLUX CHA1928
 10 CONTINUE CHA1929
 60 CONTINUE CHA1930
 DFDXI1=DRDXIX*UX+ROX*DUDXIX CHA1931
 DFDXI2=DRDXIX*UX**2+2.D0*ROX*UX*DUDXIX+DPDXIX CHA1932
 DFDXI2=DFDXI2-DPDXIX CHA1933
 DFDXI3=DUDXIX*(G12*PX+0.5D0*ROX*UX**2) CHA1934
 1 +UX*(G12*DPDXIX+0.5D0*DRDXIX*UX**2+ROX*UX*DUDXIX) CHA1935
 DFIDXI4=ZX*DFDXI1+ROX*UX*DZDXIX CHA1936
 DFDXI3=DFDXI3+QDET*DFDXI4 CHA1937
 DFIDT1=DRODTX*UX+ROX*DUDTX CHA1938
 DFIDT2=DRODTX*UX**2+2.D0*ROX*UX*DUDTX+DPDTX CHA1939
 DFIDT2=DFIDT2-DPDTX CHA1940
 DFIDT3=DUDTX*(G12*PX+0.5D0*ROX*UX**2) CHA1941
 1 +UX*(G12*DPDTX+0.5D0*DRODTX*UX**2+ROX*UX*DUDTX) CHA1942
 DFIDT4=ZX*DFIDT1+ROX*ZX*DZDTX CHA1943
 DFIDT3=DFIDT3+QDET*DFIDT4 CHA1944
 FIDOT1=-ROU00*DFDXI1+DFIDT1 CHA1945
 FIDOT2=-ROU00*DFDXI2+DFIDT2 CHA1946
 FIDOT3=-ROU00*DFDXI3+DFIDT3 CHA1947

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FIDOT4=-ROU00*DFDXI4+DFIDT4          CHA1948
UXDOT=-ROU00*DUDXIX+DUDTX          CHA1949
PXDOT=-ROU00*DPDXIX+DPDTX          CHA1950
ROXDOT=-ROU00*DRDXIX+DRODTX          CHA1951
ZXDOT=-ROU00*DZDXIX+DZDTX          CHA1952
FIH1=FI1+DT2*FIDOT1          CHA1953
FIH2=FI2+DT2*FIDOT2          CHA1954
GIH=PX+DT2*PXDOT          CHA1955
FIH3=FI3+DT2*FIDOT3          CHA1956
FIH4=FI4+DT2*FIDOT4          CHA1957
UXN=UX+DT*UXDOT          CHA1958
PXN=PX+DT*PXDOT          CHA1959
ROXN=ROX+DT*ROXDOT          CHA1960
ZRN=ZX+DT*ZXDOT          CHA1961
IF(ZRN.LT.0.) ZRN=0.          CHA1962
GO TO 90          CHA1963
20 CONTINUE          CHA1964
EV0=GL*DSQRT(BETA0)          CHA1965
201 CONTINUE          CHA1966
DFIDA1=DRODAX*UX+ROX*DUDAX          CHA1967
DFIDA2=DRODAX*UX**2+2.D0*ROX*UX*DUDAX+DPDAX          CHA1968
DFIDA2=DFIDA2-DPDAX          CHA1969
DFIDA3=DUDAX*(G12*PX+0.5D0*ROX*UX**2)          CHA1970
1    +UX*(G12*DPDAX+0.5D0*DRODAX*UX**2+ROX*UX*DUDAX)          CHA1971
DFIDA4=ZX*DFIDA1+ROX*UX*DZDAX          CHA1972
FIDOT1=-EV0*DFIDA1          CHA1973
FIDOT2=-EV0*DFIDA2          CHA1974
FIDOT3=-EV0*DFIDA3          CHA1975
FIDOT4=-EV0*DFIDA4          CHA1976
FIH1=FI1+DT2*FIDOT1          CHA1977
FIH2=FI2+DT2*FIDOT2          CHA1978
FIH3=FI3+DT2*FIDOT3          CHA1979
FIH4=FI4+DT2*FIDOT4          CHA1980
GA=DGDAX          CHA1981
IF(NFLUX.EQ.5)GA=-GA          CHA1982
DROUA=UX*DRODAX+ROX*DUDAX          CHA1983
BETAPR=0.5D0*DSQRT(BETA0)*(GA-DROUA)          CHA1984
FIH2=FI2-DPDBX*BETAPR*DT2          CHA1985
UXDOT=-EV0*DUDAX+BETAPR*DUDBX          CHA1986
PXDOT=-EV0*DPDAX+BETAPR*DPDBX          CHA1987
GIH=PX+DT2*PXDOT          CHA1988
ROXDOT=-EV0*DRODAX+BETAPR*DRODBX          CHA1989
ZXDOT=-EV0*DZDAX          CHA1990
UXN=UX+DT*UXDOT          CHA1991
PXN=PX+DT*PXDOT          CHA1992
ROXN=ROX+DT*ROXDOT          CHA1993
ZRN=ZX+DT*ROXDOT          CHA1994
IF(ZRN.LT.0.) ZRN=0.          CHA1995
GO TO 90          CHA1996
50 CONTINUE          CHA1997
EV0=-GR*DSQRT(BETA0)          CHA1998
GO TO 201          CHA1999
30 CONTINUE          CHA2000
40 CONTINUE          CHA2001
GO TO 60          CHA2002
90 CONTINUE          CHA2003
RETURN          CHA2004
END          CHA2005

```

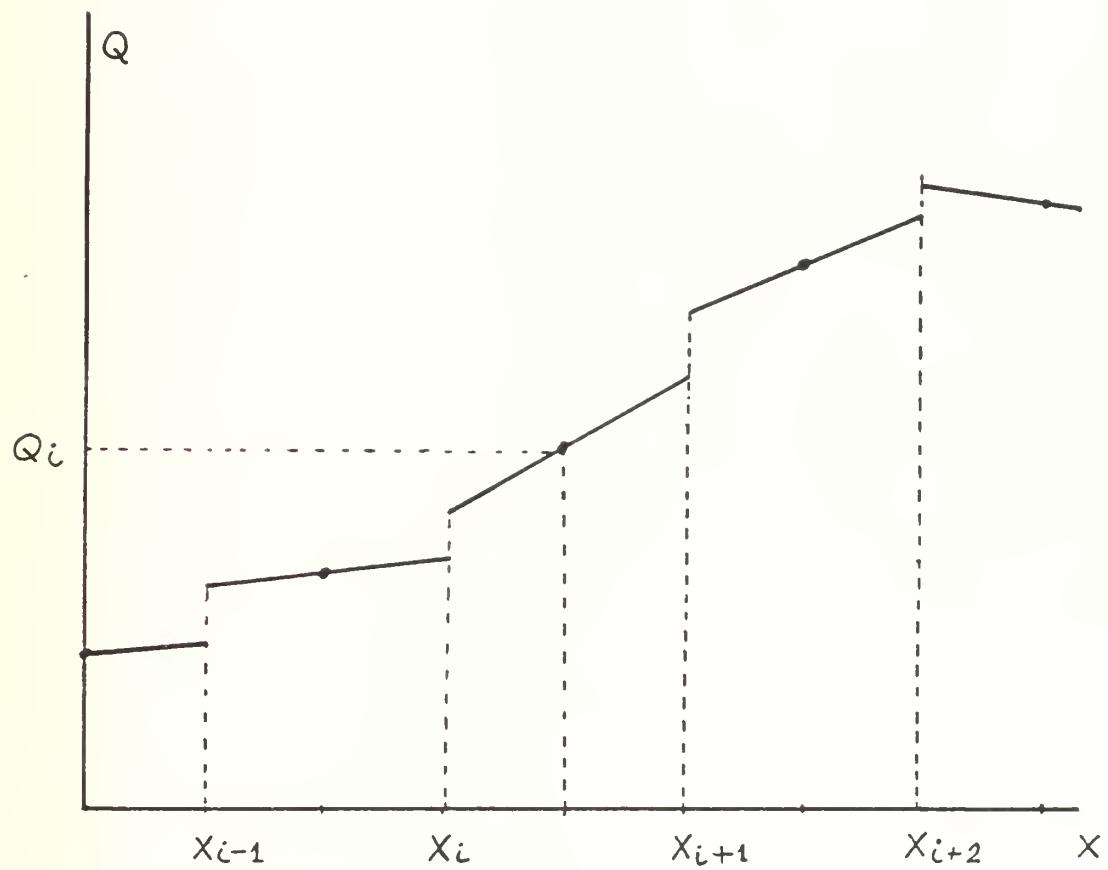


Figure A-1. Piecewise Linear Distribution of Flow Variables in Cells

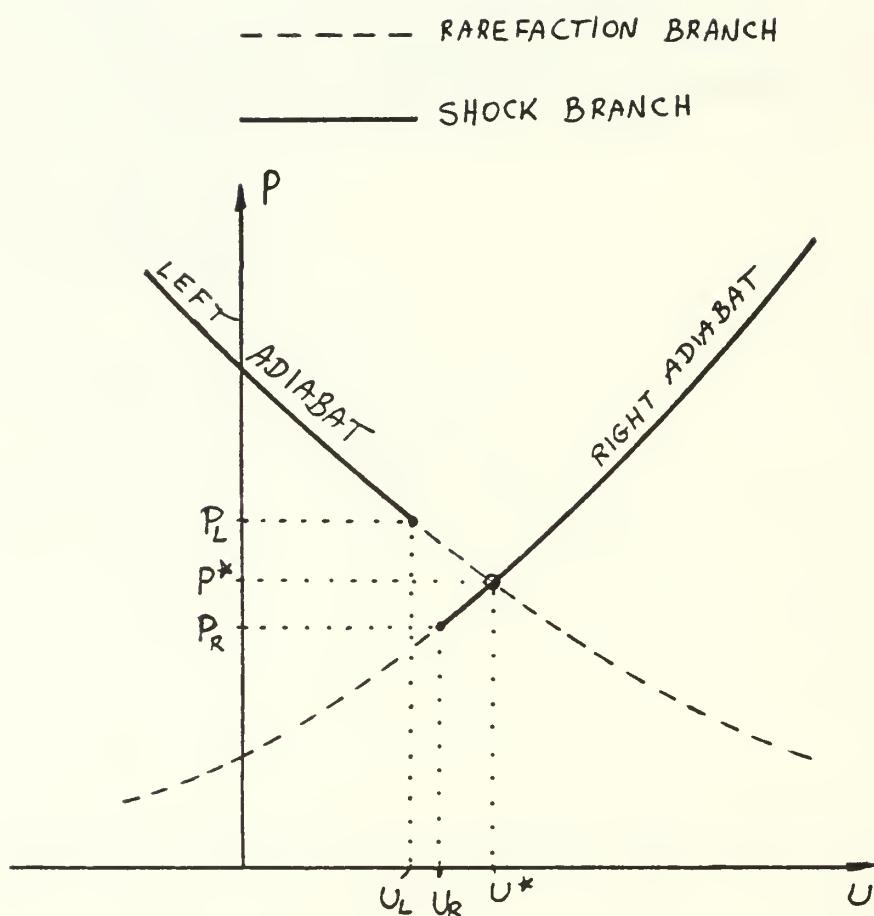


Figure A-2. Intersection of Right and Left Adiabats for Solving Riemann Problem

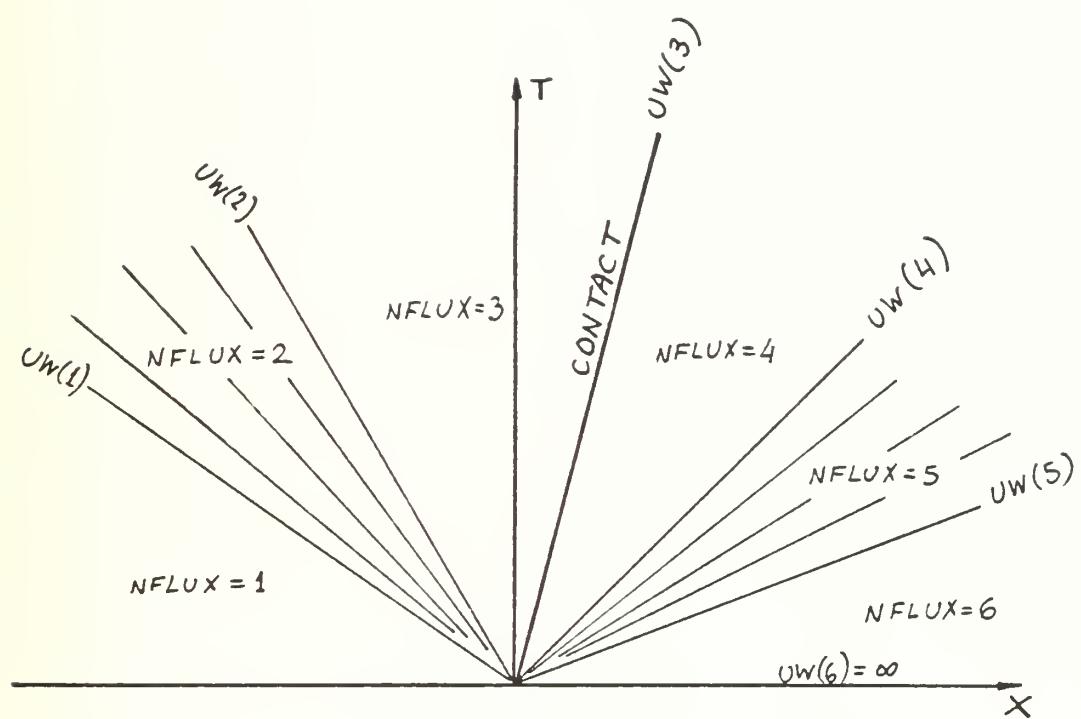


Figure A-3. Wave Diagram Representing Solution to Riemann Problem

APPENDIX B. Code for Re-Normalizing the Air Impulse

```

1      IMPLICIT REAL*8(A-H,O-Z)          REN00
2      C  CODE RENORM -- C  TRANSFORMATION OF TOTAL REFLECTED IMPULSE FROM
3      C  BAKER'S CHART TO SPACE-NORMALIZED VALUES.          REN00
4      C  DATA FROM FIG. 6.3 (SUPPLEMENT) IN BAKER'S BOOK "EXPLOSIONS IN AIR" REN00
5      REAL*4 RB,IB,RS,IS,ISBARE          REN00
6      DIMENSION RB(21),IB(21)          REN00
7      DIMENSION RS(21),IS(21),ISBARE(21)          REN00
8      DATA RB/.05,.06,.07,.08,.09,.1,.2,.3,.4,.5,.6,.7,.8,.9,1.,
9          1          2,.3,.4,.5,.6,.7./          REN00
10     DATA IB/4.4,3.06,2.30,1.83,1.50,1.27,.457,.293,.221,.178,.149,
11          1          .128,.113,.099,.0885,.0376,.0236,.0173,.0136,.0113,.0095/ REN00
12     PAI=4.D0*DATAN(1.D0)          REN00
13     G=1.4D0          REN00
14     PA=0.1D0          REN00
15     RHOA=1.3D0          REN00
16     RH00=1800.D0          REN00
17     Q0=4.D0          REN00
18     BETA=DSQRT(RHOA/RH00)*(PA/(RH00*Q0))**((1.D0/6.D0)          REN00
19     GOREM=(3.D0/DSQRT(2.D0*G))*((4.D0*PAI/3.D0)**(1.D0/3.D0)          REN00
20     BETA=BETA*GOREM          REN00
21     DELTA=((4.D0*PAI/3.D0)*(RH00*Q0/PA))**((1.D0/3.D0)          REN00
22     PRINT 11, BETA,DELTA          REN00
23     11 FORMAT(1X,'RESULTS WITH BETA,DELTA=',2D16.7//          REN00
24     1          1X,' N', ' RB', ', ' IB', ', 2X,          REN00
25     2          ' RS', ', ' IS', ', 2X, ' ISBARE ', '/')          REN00
26
19     DO 1 N=1,21          REN00
20     RS(N)=RB(N)*DELTA          REN00
21     IS(N)=IB(N)*BETA          REN00
22     ISBARE(N)=1.D0/RS(N)**2          REN00
23     PRINT 2, N, RB(N), IB(N), RS(N), IS(N), ISBARE(N)          REN00
24     2 FORMAT(1X,I4,2E12.4,2X,2E12.4,2X,E12.4)          REN00
25     1 CONTINUE          REN00
26     END          REN00

```

RESULTS WITH BETA,DELTA= 0.1204163D-01 0.6706157D+02

N	RB	IB	RS	IS	ISBARE
1	0.5000E-01	0.4400E+01	0.3353E+01	0.5298E-01	0.8894E-01
2	0.6000E-01	0.3060E+01	0.4024E+01	0.3685E-01	0.6177E-01
3	0.7000E-01	0.2300E+01	0.4694E+01	0.2770E-01	0.4538E-01
4	0.8000E-01	0.1830E+01	0.5365E+01	0.2204E-01	0.3474E-01
5	0.9000E-01	0.1500E+01	0.6036E+01	0.1806E-01	0.2745E-01
6	0.1000E+00	0.1270E+01	0.6706E+01	0.1529E-01	0.2224E-01
7	0.2000E+00	0.4570E+00	0.1341E+02	0.5503E-02	0.5559E-02
8	0.3000E+00	0.2930E+00	0.2012E+02	0.3528E-02	0.2471E-02
9	0.4000E+00	0.2210E+00	0.2682E+02	0.2661E-02	0.1390E-02
10	0.5000E+00	0.1780E+00	0.3353E+02	0.2143E-02	0.8894E-03
11	0.6000E+00	0.1490E+00	0.4024E+02	0.1794E-02	0.6177E-03
12	0.7000E+00	0.1280E+00	0.4694E+02	0.1541E-02	0.4538E-03
13	0.8000E+00	0.1130E+00	0.5365E+02	0.1361E-02	0.3474E-03
14	0.9000E+00	0.9900E-01	0.6036E+02	0.1192E-02	0.2745E-03
15	0.1000E+01	0.8850E-01	0.6706E+02	0.1066E-02	0.2224E-03
16	0.2000E+01	0.3760E-01	0.1341E+03	0.4528E-03	0.5559E-04
17	0.3000E+01	0.2360E-01	0.2012E+03	0.2842E-03	0.2471E-04
18	0.4000E+01	0.1730E-01	0.2682E+03	0.2083E-03	0.1390E-04
19	0.5000E+01	0.1360E-01	0.3353E+03	0.1638E-03	0.8894E-05
20	0.6000E+01	0.1130E-01	0.4024E+03	0.1361E-03	0.6177E-05
21	0.7000E+01	0.9500E-02	0.4694E+03	0.1144E-03	0.4538E-05

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